

# Study on acoustic fault diagnosis of underwater vehicle auxiliary machineries

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**Abstract.** The concept of underwater vehicle auxiliary machineries acoustic fault was proposed. The underwater vehicle auxiliary machineries acoustic fault diagnosis in concealed conditions was studied. Firstly, the accelerometers were used to measure the vehicle shell surface vibration, and the vehicle radiation noise was calculated using a rapid engineering estimation method. Then, the vibration energy of each frequency band in the radiation noise analysis frequency was extracted as feature vector. Finally, an improved Fuzzy Support Vector Machine (FSVM) method was used to identify the classification, and acoustic fault diagnoses of auxiliary machineries for underwater vehicle was given. The method of acoustic fault diagnosis proved a theoretical basis for the use of underwater vehicle auxiliary machineries under the concealment.

**Keywords:** underwater vehicle auxiliary machineries, acoustic fault diagnosis, FSVM.

## 1. Introduction

The stealth property of underwater vehicle in sea battlefield is the most basic technical performance, where acoustic stealth performance is the most important factor in determining its stealth. The acoustic stealth performance of underwater vehicle has always been considered to be the most important issue [1]-[4].

The radiation noise of underwater vehicle can be divided into three kinds: machineries noise, propeller noise, hydrodynamic noise [5]. When the underwater vehicle is sailing, the propeller noise and the hydrodynamic noise occupy the main part. But when it is in concealed conditions such as “position for ambush”, “regional hunting” and so on, underwater vehicle should be in hover condition. And in these time, the host and propeller are both stopped. The propeller noise and the hydrodynamic noise disappear, and the radiation noise of the vehicle is only the mechanical noise. At these times, the main noise sources are auxiliary machineries, which mainly includes various types of pumps, air conditioners, refrigeration, hydraulic devices and so on. Now if the radiation noise is abnormal due to the incorrect use of auxiliary machineries, the acoustic stealth performance of the vehicle is changed, and its security is destroyed. This is called the acoustic fault of auxiliary machineries.

Define “underwater vehicle auxiliary machineries acoustic fault” as: in sea battlefield, when underwater vehicle auxiliary machineries vibration or noise changes due to improper use or state change, resulting in changing vehicle stealth properties. It should be noted that the auxiliary mechanical acoustic fault does not mean that the auxiliary machineries has a mechanical fault and needs to be repaired.

“Underwater auxiliary mechanical acoustic fault diagnosis” is: when the underwater vehicle auxiliary machineries are mainly used, the current acoustic stealth state elements are perceived and extracted, and they map them into existing state spaces, get some kind the matching of known states, and determines its acoustic fault state. The state here can be quantized indicators (like 60 points, 90 points, etc.), or may be a hierarchical evaluation (like no acoustic fault, slight acoustic fault, severe acoustic fault, etc.).

It should be noted that underwater vehicle auxiliary mechanical acoustic fault diagnosis is

mainly carried out under hover condition or slow sailing. Because in these time vehicle has higher requirements for stealth, and machineries noise is the main part of radiation noise. When the vehicle is at a high speed, the maneuverability requirement is higher than stealth. In these time, the propeller noise and hydrodynamic noise are much louder than machineries noise, so the auxiliary mechanical acoustic fault diagnosis is not necessary.

## 2. Rapid calculation method of underwater vehicle radiation noise in concealed conditions

The first step in the diagnosis is to quickly calculate the radiation noise, which is made by auxiliary machineries, by using the vibration measured by the sensors on the vehicle. An engineering estimation method of rapid calculating underwater vehicle radiation noise in concealed conditions has been proposed [6], [7]. The radiation noise is [7]:

$$P = \frac{\rho_0 c_0 \langle \bar{V} \rangle}{2R} \sqrt{\frac{\varepsilon S}{\pi}} = \frac{\rho_0 c_0 \langle \bar{\zeta} \rangle}{2\omega R} \sqrt{\frac{\varepsilon S}{\pi}}, \quad (1)$$

where,  $P$  is the sound pressure of radiation noise at a distance of  $R$  from the vehicle;  $\rho_0$ ,  $c_0$  are the density and sound speed of water;  $\langle \bar{V} \rangle$  is the average vibration speed of the vehicle surface;  $\langle \bar{\zeta} \rangle$  is the average vibration acceleration of the vehicle surface;  $S$  is the acoustic radiation surface area of the vehicle;  $\varepsilon$  is the radiation efficiency of the vehicle:

$$10\lg\varepsilon = \begin{cases} 40(\lg f - \lg f_m), & f \leq f_1, \\ 20(1 + K)\lg f + 20(1 - K)\lg f_1 - 40\lg f_m, & f_1 < f < f_c, \\ 0, & f \geq f_c, \end{cases} \quad (2)$$

where,  $f$  is a calculation frequency;  $K = \frac{\lg(f_m^2)/(f_c f_1)}{\lg(f_c f_1)}$ ;  $f_1$  is the first order of vibration modal frequency of the cylindrical vehicle:

$$f_1 = \begin{cases} 2.66f_r\beta, & \left(\frac{d}{l}\right)^2 \geq 0.6\left(\frac{h}{d}\right), \\ \frac{\pi d f_r}{2l} \sqrt{\left(\frac{\pi d}{2l}\right)^2 + 2\beta^2}, & \left(\frac{d}{l}\right)^2 < 0.6\left(\frac{h}{d}\right). \end{cases} \quad (3)$$

Critical frequency  $f_c$  is:

$$f_c = \frac{c_0^2}{2\pi h} \sqrt{\frac{12\rho(1 - \sigma^2)}{E}} = \frac{2\sqrt{3}R_{cp}}{h} \left(\frac{c_0}{c_l}\right)^2 f_r. \quad (4)$$

In the real underwater vehicle radiation noise calculation, lots of accelerometers are arranged on the surface of the vehicle. The sound pressure of each cabin is considered independent. The length of  $i$ -th cabin is  $l_i$ , and the equivalent radius is  $r_i$ . It can be obtained from Eqs. (1-4) that the total sound pressure, which is made by the underwater vehicle multi-cabin vibration, at a distance

of  $R$  from the vehicle is  $P_\Sigma = \sum_i \frac{\rho_0 c_0 \langle \bar{\zeta} \rangle}{\omega R} \sqrt{\frac{\varepsilon_i r_i l_i}{2}}$ .

Translates to the total sound pressure at a distance of 1m from the vehicle is:

$$P_{\Sigma} = \sum_i \frac{\rho_0 c_0 \langle \bar{\zeta} \rangle}{\omega} \sqrt{\frac{\varepsilon_i r_i l_i}{2}}. \quad (5)$$

If the energy of radiation noise is mostly concentrated from  $f_{down}$  to  $f_{up}$  frequency range, each 1/3Oct sound pressure levels of the frequency range can be arranged to the feature vectors.

Using this underwater vehicle radiation feature vectors, the pattern recognition can be performed by the fuzzy support vector machine (FSVM) to make the auxiliary mechanical acoustic fault diagnosis.

### 3. FSVM for diagnosis of two modes

If the auxiliary machine acoustic fault category is simple to be two: occurring and not occurring, the acoustic fault diagnosis problem is an identification issue of two model classes. Under the conditions of complete linearity, ordinary linear support vector machines (SVM) are suitable for this problem [8]. However, in actual underwater vehicle auxiliary machineries acoustic fault diagnosis, the sample is almost not completely linear, so the nonlinear SVM must be used. And sometimes, not all training samples are valid. Some the validity of samples may be weakened or even be corrupted in actual underwater vehicle auxiliary machineries acoustic fault diagnosis. For such problems, the FSVM method has been proposed [9], [10].

#### 3.1. Linear FSVM for diagnosis of two patterns

In order to solve non-separable data, a set of new non-negative scalar variables  $\xi_i$  ( $i = 1, 2, \dots, l$ ) are introduced to the definition of the separation super plane:

$$y_i(w^T x_i + b) \geq 1 - \xi_i, \quad i = 1, 2, \dots, l, \quad (6)$$

where,  $\xi_i$  is a relaxation variable, which measures the data deviation degree of the ideal condition of separable pattern. Support vector is the special data that exactly satisfied Eq. (6). For linear classification problems, the problem of searching for the optimal classification super plane can be transform to solve the Eq. (7):

$$\begin{cases} \text{minimize} & \frac{1}{2} \|w\|^2 + C \sum_{i=1}^l s_i \xi_i, \\ \text{subject to} & y_i(w^T x_i + b) \geq 1 - \xi_i, \quad i = 1, 2, \dots, l, \\ & \xi_i \geq 0, \quad i = 1, 2, \dots, l. \end{cases} \quad (7)$$

That is, a fault classification support vector with a smaller degree of fuzzy membership is considered less important in the classification problem. The Lagrange multiplier method can be used to solve this optimization problem. Constructing the Lagrange function as:

$$L(w, b, \xi, \alpha, \beta) = \frac{1}{2} \|w\|^2 + C \sum_{i=1}^l s_i \xi_i - \sum_{i=1}^l \alpha_i (y_i(w^T x_i + b) - 1 + \xi_i) - \sum_{i=1}^l \beta_i \xi_i. \quad (8)$$

The solution to the optimization problem is determined by the saddle points of the Lagrange function. When the cost function  $\frac{1}{2} \|w\|^2 + C \sum_{i=1}^l s_i \xi_i$  takes the extreme value, by Karush-Kuhn-Thcker condition. The dual programming of the quadratic programming Eq. (7) can be converted to solving for the minimum as:

$$\left\{ \begin{array}{l} \text{minimize } \alpha \quad \frac{1}{2} \sum_{i=1}^l \sum_{j=1}^l y_i y_j \alpha_i \alpha_j (x_i^T x_j) - \sum_{i=1}^l \alpha_i, \\ \text{subject to } \quad \sum_{i=1}^l y_i \alpha_i = 0, \\ \quad \quad \quad 0 \leq \alpha_i \leq s_i C, \quad i = 1, 2, \dots, l. \end{array} \right. \quad (9)$$

The optimal solution of  $w$  and  $b$  are:

$$w^* = \sum_{i=1}^l \alpha_i^* y_i x_i, \quad (10)$$

$$b^* = y_i - \sum_{j=1}^l y_j \alpha_j (x_j^T x_i), \quad i \in \{i | 0 < \alpha_i^* < s_i C\}. \quad (11)$$

The fuzzy optimal classification function is:

$$g(x) = \text{sgn}\{f(x)\} = \text{sgn}\{(w^{*T} x) + b^*\}, \quad x \in R^n. \quad (12)$$

### 3.2. Nonlinear FSVM for diagnosis of two patterns

For nonlinear classification issues, it is usually used by nonlinear mapping from low dimensional spaces to high dimension  $\varphi(\cdot): R^d \rightarrow R^{dh}$ , and transforms nonlinear problems in low dimensional spaces into linear problems in high dimensional spaces. Inner product operation in high dimensional space is defined as  $K(x_i, x_j) = \varphi(x_i)^T \varphi(x_j)$ , and it is called kernel function [11]. So the issues of seeking the optimal classification hyperplane can be transformed to solving the quadratic programming. The solution process is the same as in Section 2.1, and the following dual planning can be obtained:

$$\left\{ \begin{array}{l} \text{minimize } \alpha \quad \frac{1}{2} \sum_{i=1}^l \sum_{j=1}^l y_i y_j \alpha_i \alpha_j K(x_i, x_j) - \sum_{i=1}^l \alpha_i, \\ \text{subject to } \quad \sum_{i=1}^l y_i \alpha_i = 0, \\ \quad \quad \quad 0 \leq \alpha_i \leq s_i C, \quad i = 1, 2, \dots, l. \end{array} \right. \quad (13)$$

Similarly, the optimal solution is  $\alpha^* = (\alpha_1^*, \alpha_2^*, \dots, \alpha_l^*)^T$ , and the fuzzy optimal classification function is:

$$g(x) = \text{sgn}\{f(x)\} = \text{sgn}\left\{ \sum_{j=1}^l \alpha_j^* y_j K(x, x_j) + b^* \right\}, \quad x \in R^n. \quad (14)$$

where  $b^* = y_i - \sum_{j=1}^l y_j \alpha_j K(x_j, x_i)$ ,  $i \in \{i | 0 < \alpha_i^* < s_i C\}$ .

Polynomial function, radial basis function, sigmoid function are often used as kernel functions. To a specific problem, how to choose the optimal kernel function and the corresponding parameters are a complex problem to FSVM. Although the choice of kernel functions can lead to different performances, the choice of parameters is more important than the choice of kernel functions. In many cases, the choice of the kernel function parameters is decisive to the result [11].

#### 4. FSVM for diagnosis of multi-patterns

In the actual underwater vehicle auxiliary machineries acoustic fault diagnosis, the acoustic fault patterns are usually more than two. So underwater vehicle auxiliary machineries acoustic fault diagnosis is a multi-pattern classification problem. For more than two patterns ( $n > 2$ ), it can be constructed as a combination of multiple two-pattern classification issues [12]-[13].

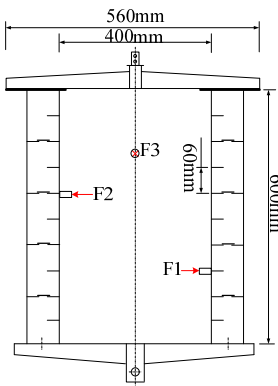
Using two patterns classification methods,  $n$ -pattern classifier can be constructed as follow:

1. Construct  $n$  two-pattern classification rules, where the rule  $f_k(x)$ ,  $k = 1, \dots, n$  separates the training samples of the  $k_{th}$ -pattern from other training samples. (If the vector  $x_i$  belongs to the  $k_{th}$ -pattern,  $g_k(x_i) = \text{sgn}\{f_k(x_i)\} = 1$ ; otherwise  $g_k(x) = \text{sgn}\{f_k(x_i)\} = -1$ ).

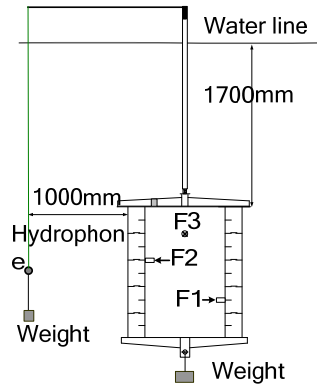
2. If the patterns satisfy  $g_k(x) = \text{sgn}\{f_k(x)\} = 1$  are more than one,  $x$  becomes the pattern  $m = \text{argmax}\{f_1(x), \dots, f_k(x)\}$  that is corresponding to the maximum value of the function  $f_k(x)$ ,  $k = 1, \dots, n$ . If all the patterns satisfy  $g_k(x) = \text{sgn}\{f_k(x)\} = -1$ ,  $x$  becomes the pattern  $m = \text{argmin}\{f_1(x), \dots, f_k(x)\}$  that is corresponding to the minimum value of the function  $f_k(x)$ ,  $k = 1, \dots, n$ .

#### 5. Test verification

In order to verify the FSVM diagnosis method, underwater acoustic tests are performed using a double-shell iron cylinder to simulate underwater vehicle under hover condition. The outer diameter of the cylinder is 560 mm, the inner diameter is 400 mm, and the height is 600 mm. Three exciters are mounted inside the housing to simulate the excitation of the auxiliary mechanicals, and 15 accelerometers are arranged on the surface of the cylinder, as shown in Fig. 1. A hydrophone suspended in the water is 1m from the cylinder, as shown in Fig. 2.



**Fig. 1.** Iron cylinder with covers and accelerometers, F1, F2, F3 are the excitation points of exciters



**Fig. 2.** Underwater acoustic test

Without loss of generality, the auxiliary mechanical acoustic fault states can be classified into three patterns for diagnosis, namely: safety, normal fault, critical fault. They correspond to three conditions in the test: Condition (1) turn on No. 1 exciters, Condition (2) turn on No. 1 and 2 exciters, Condition (3) turn on all the three exciters.

To verify the correctness of the algorithm in Chapter 1, a random set of data is selected for calculation in each condition. And calculation results are compared with the hydrophone measurement, as shown in Fig. 3-5.

As Table 1 shows, for our test linear FSVM and polynomial kernel function FSVM gets high accuracy in acoustic fault diagnosis. This is because the system is largely linear. However, the actual underwater vehicle has so many different kinds of auxiliary machineries, and underwater environment is so complicated, that the system cannot be considered as linear. So it is impossible to predict which type of FSVM will give better diagnosis results.

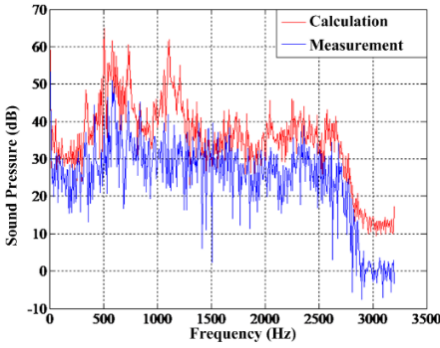


Fig. 3. Comparison in Condition (1)

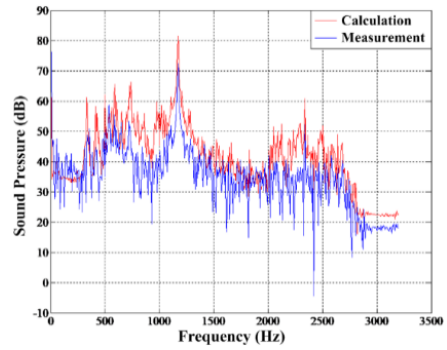


Fig. 4. Comparison in Condition (2)

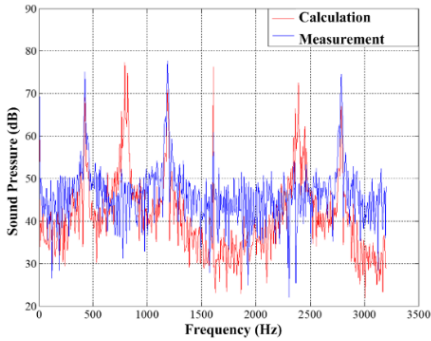


Fig. 5. Comparison in Condition (3)

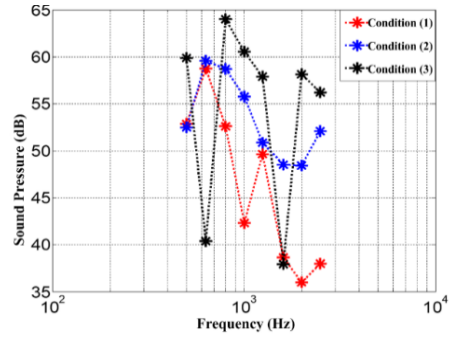


Fig. 6. Each band sound pressure in three conditions

Table 1. Comparison of different FSVM classification accuracy

Type of FSVM	Diagnosis accuracy (%)
Linear FSVM	100
Polynomial Kernel Function FSVM	93.75
Radial Basis Kernel Function FSVM	33.3
Sigmoid Kernel Function FSVM	33.3

## 6. Conclusions

In the paper the concept of underwater vehicle auxiliary machineries acoustic fault has been proposed, and the auxiliary machineries acoustic fault diagnosis in sea battlefield has been studied. It should be noticed that: (1) for different underwater vehicle structures, the FSVM classifier needs to be trained with historical data; (2) in actual underwater vehicle auxiliary machineries acoustic fault diagnosis, the selection of FSVM classifier kernel function should be according to the situation; (3) as the auxiliary machineries acoustic fault patterns increase, the amount of FSVM calculation will increase rapidly, which increases the diagnosis time; (4) the noise prediction accuracy of the underwater vehicle radiation noise engineering estimation algorithm needs to be improved in individual frequency bands.

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