# Design of a high-payload Mecanum-wheel ground vehicle (MWGV)

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Abstract. With the rapid developments of Industry 4.0 and Smart Manufacturing, customized manufacturing has been becoming greatly needed. Meanwhile, the challenge of production automation has become more bigger, especially for the automation of moving, picking, placing and manipulating objects. Many researchers have begun to work on Autonomous Ground Vehicles (AGVs). Most AGVs were utilized to carry middle or small objects, as the high-payload AGVs were rarely developed. This paper focused on the design of a High-Payload Mecanum-Wheel Ground Vehicle (MWGV), which was 1.7 m wide and 2.04 m long. The weight of the vehicle was 740 kg and it was able to carry the payload as its own weight (i.e. around 7,300 N). The safety factor of the structural strength was greater than 1.66 and the safety factor of the axial design was at least 6.24. The vehicle was designed to carry 150-kg weight with a reach of 1.375 m without falling. The design of Mecanum wheels provided great flexibility on movement with small rotational radius. Mathematical descriptions about how Mecanum wheels were controlled was also introduced in this paper. Furthermore, the mechatronics and software integrations were demonstrated. The final experimental results showed the developed MWGV was able to perform the desired movement properly.

**Keywords:** mechanical design, mechatronics, Mecanum wheel, autonomous ground vehicle.

#### 1. Introduction

Autonomous ground vehicles (AGVs) [1-9] have been developed for industrial applications and began to play important roles in the development of Industry 4.0 and Smart Manufacturing. AGV could be used for carrying and moving items in the factory replacing some of the labor-intensive human missions. On the other hand, linear (or curved) guideways have been widely used for the similar purposes and functions as AGV. Linear guideways could provide high payload capability but the moving trajectories are usually fixed. Fig. 1 shows a robot arm system with linear guideway that could be moving along the given linear trajectory freely and picking/placing items at the surrounding elements. The Erowa ERG150L robot arm could be moving in a 30 m long linear guideway and reach out for 1.375 m long to carry a 150 kg item without falling over. The linear layout could be customized based on the needs but rearranging the layout could take some time. Rearrangement of the layout won't happen too often; therefore, the robot arm system with linear guideway is not as flexible as robot arm on an AGV, which can move freely inside the factory.

Table 1 shows a list of commercial AGV. There are two kinds of AGVs: the first kind is for carrying heavy objects and the other kind is designed for robot arm manipulation. As shown in Table 1, Symbridge MiR1000 could carry 1000-kg payload as the iAmech 2D Bar Code Guide

AGV could carry 300 kg payload. Prefactortech MR-VT6 has a robot arm with a 6 kg payload and GreenTrans MR-100 carries a robot arm with 12 kg payload. The AGV with robot arm usually has a lower capability of carrying weights because its center of mass is typically higher than the AGV without robot arm and lower payload prevents the chance of falling over. Therefore, AGV with a high-payload robot arm is less common in the market. This paper presents a AGV that is designed for carrying a high-payload robot arm. The goal of this design is to manipulate heavy objects in a mobile system that could freely move (and rotate) inside a smart factory.



Fig. 1. Erowa robot arm system with linear guideway [10]

Table 1. Comparison of commercial AGVs

| Table 1. Comparison of commercial 116 vs |                 |                       |                |                |
|--|-----------------|-----------------------|----------------|----------------|
| Company                                  | Symbridge group | iAmech                | Prefactortech  | GreenTrans     |
| Product name                             | MiR1000         | 2D Bar Code Guide AGV | MR-VT6         | MR-100         |
| Carrying payload                         | 1000 kg         | 300 kg                | 70 kg          | 100 kg         |
| Robot arm                                | No              | No                    | Yes            | Yes            |
| Robot arm payload                        | -               | _                     | 6 kg           | 12 kg          |
|  | Length 1350 mm  | Length 850 mm         | Length 1154 mm | Length 1154 mm |
| Size of vehicle                          | Width 920 mm    | Width 650 mm          | Width 654 mm   | Width 654 mm   |
|  | Height 320 mm   | Height 305 mm         | Height 700 mm  | Height 700 mm  |
| Weight of vehicle                        | 231 kg          | 110 kg                | 230 kg         | 242 kg         |

## 2. Mechanical design of the MWGV

In this paper, the design of a high-payload Mecanum-Wheel Ground Vehicle (MWGV) [11, 12] is presented. The goal of the proposed MWGV is to integrate with a parallel platform, a high-payload robot arm, and a gravity compensation design, as shown in Fig. 2. The parallel platform ensures that the coordinate system of the robot arm above the platform aligns with the direction of gravity even when the ground is not completely flat. Although the gravity compensation system increases the external loads applied to some of the axis motors in the robot arm, it enhances the capability of manipulating the objects that are heavier than the allowable payload. The mechanical design and analysis of the MWGV will be introduced in this section.

## 2.1. Mechanical design of the chassis and the axle systems

Fig. 3 shows the mechanical design of the proposed MWGV, which is 1.7 m in length, 2.04 m in width and 0.4 m in height. The length of the vehicle (from front to back) is shorter than the width (from left to right) so that robot manipulation could be done at the frontal direction of the vehicle. The total weight of the MWGV is 740 kg, which is heavy enough so that the robot arm above it could carry a 150-kg object in a reach of 1.375 m without falling over. The vehicle is composed of a chassis, 4 axle systems and other circuit components. The axle system, as shown in Fig. 4, is powered by the battery, shown in Fig. 3 (j). A driver, shown in Fig. 3 (i), transmits

motor control signals to one motor, that is connected to a reducer, as shown in Fig. 3 (h). The motor shaft is connected to a wheel axle, Fig. 4 (c), using a set of coupling rubbers, Fig. 4 (b). The wheel axle is carried by two ball bearings, as shown in Fig. 4 (a). One Mecanum wheel is fixed to the axle using a fixing ring, as shown in Fig. 4 (d), and tightened with a bolt and a washer, as shown in Fig. 4 (e), at the edge of the axle. The batteries are connected to a circuit system with multiple copper ground bars, as shown in Fig. 3 (k), and a fuesless breaker, as shown in Fig. 3 (l).

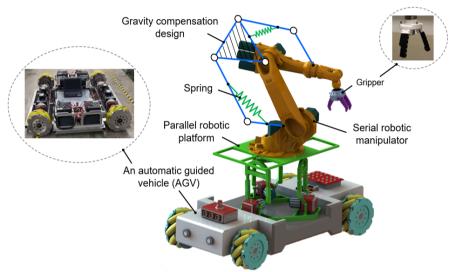


Fig. 2. Design of a high-payload ground vehicle with robot manipulation for industrial applications

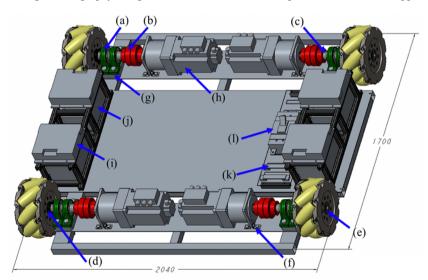


Fig. 3. The mechanical design of the MWGV: (a) ball bearing, (b) coupling rubber, (c) axle, (d) fixing ring, (e) washer, (f) L-shaped bracket, (g) metal plate, (h) motor and reducer, (i) driver, (j) battery, (k) copper ground bar, (l) fuseless breaker

The commercially available mechanical parts include the bearings, coupling rubbers, motors, and reducers. On the other hand, the chassis and axles were designed based on stress analyses and evaluations of safety factors. Fig. 5 shows the Finite Element Analysis (FEA) of the chassis design. The chassis, that is made of S45C steel, carries a uniformly distributed load of 7300 N at the center (around same as the vehicle's own weight), as shown in Fig. 5 (a). Each battery applies

an external load of 200 N (totally 800 N) to the chassis and each motor system applies a load of 500 N (totally 2000 N). The FEA results are shown in Table 2. The maximum von Mises stress was found at the center of the chassis, as shown in Fig. 5 (b), and its magnitude was 193.92 MPa. Based on Maximum Distortion Energy (MDE) Theory [13], the safety factor could be calculated by maximum von Mises stress over the yielding strength, 343.23 MPa and it was 1.77, as shown in Table 3. The maximum shear stress was found to be 103.50 MPa. Based on Maximum Shear Stress (MSS) Theory [13], safety factor (i.e. maximum shear stress divided by two times yielding strength) was 1.66. The maximum displacement of the chassis was 3.03 mm. Fig. 6 shows the FEA of the wheel axle, that is also made of S45C steel. Each axle carries one fourth of the sum of the vehicle weight and the payload placed at the center of the chassis, i.e. 3626 N. The stress concentration was found near the edge of the bearing, as shown in Fig. 6 (b). The maximum von Mises stress and shear stresses in the axle were found to be 49.04 and 27.52 MPa, respectively. Therefore, the safety factors for the static load condition were 7.00 (based on MDE) and 6.24 (based on MSS), respectively. Wheel axles of AGV do not rotate as fast and frequently as other rotary systems so it's not essential to perform fatigue analysis due to fluctuating loads.

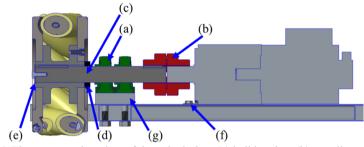


Fig. 4. The cross-section view of the axle design: (a) ball bearing, (b) coupling rubber, (c) axle, (d) fixing ring, (e) washer, (f) L-shaped bracket, (g) metal plate

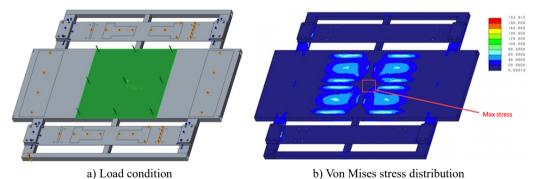


Fig. 5. FEA of the chassis

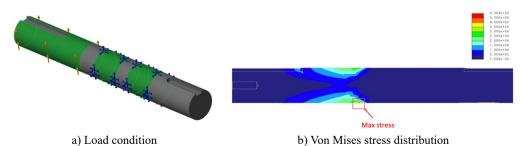


Fig. 6. FEA of the axle

Table 2. FEA results

| Simulation results   | Stress in chassis | Stress in axle |
|----------------------|-------------------|----------------|
| Max von Mises stress | 193.92 MPa        | 49.04 MPa      |
| Max shear stress     | 103.50 MPa        | 27.52 MPa      |
| Max displacement     | 3.03 mm           | 0.06 mm        |

Table 3. Safety factors of chassis and axle

| Safety factor models | Safety factors of chassis | Safety factors of axle |
|----------------------|---------------------------|------------------------|
| MDE                  | 1.77                      | 7.00                   |
| MSS                  | 1.66                      | 6.24                   |

## 2.2. Design of the Mecanum wheels

A Mecanum wheel is known to have multiple rollers around its perimeter, as shown in Fig. 7. The diameter of each wheel is 375 mm and the weight is 71 kg. The rotational axis of the roller as a 45-degree twist against the wheel axis. The friction force between the roller and the ground is not along the frontal direction of the vehicle; therefore, the transverse part of the friction force allows the vehicle to move from left to right. The separate control of each Mecanum wheel allows the vehicle to move and rotate freely.

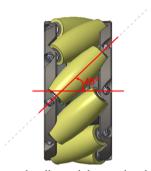


Fig. 7. Twist angle between each roller and the rotational axis of the Mecanum wheel

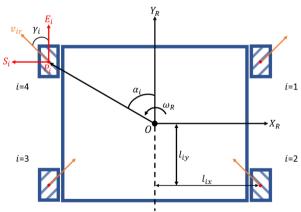


Fig. 8. Arrangement of the four Mecanum wheels

The layout of the Mecanum wheels is shown in Fig. 8. **0** is the center of the vehicle.  $\mathbf{X}_R$  and  $\mathbf{Y}_R$  are the transverse and front directions of the vehicle, respectively. The velocity vectors of the vehicle along the  $\mathbf{X}_R$  and  $\mathbf{Y}_R$  directions are given as  $\mathbf{v}_{X_R}$  and  $\mathbf{v}_{Y_R}$ , respectively. The angular velocity of the vehicle is  $\omega_R$ . i stands for the index of the Mecanum wheel.  $\mathbf{P}_i$  is the center of the ith wheel. The distance from  $\mathbf{0}$  to  $\mathbf{P}_i$  is given as  $l_i$ . The horizontal and vertical distances from  $\mathbf{0}$ 

to  $\mathbf{P}_i$  are given as  $l_{ix}$  and  $l_{iy}$ , respectively. The angle from  $\mathbf{P}_i$  to  $\mathbf{Y}_R$  is denoted as  $\alpha_i$ . More details about the wheel could be seen in Fig. 9. The velocity vector of the roller of the *i*th wheel is given as  $\mathbf{v}_{ir}$ .  $\mathbf{S}_i$  and  $\mathbf{E}_i$  represent the axial and transverse direction of the wheel, respectively. The components of  $\mathbf{v}_{ir}$  along the directions of  $\mathbf{S}_i$  and  $\mathbf{E}_i$  are given as  $\mathbf{v}_{S_i}$  and  $\mathbf{v}_{E_i}$ , respectively. The angle between  $\mathbf{E}_i$  and  $\mathbf{v}_{ir}$  is  $\gamma_i$ . The radius of the tire is  $r_i$  and the radius of the roller is  $r_i$ . The angle between the wheel coordinate and the vehicle coordinate is  $\beta_i$ . The angular velocity and moving speed of the *i*th wheel are denoted as  $\omega_i$  and  $w_{E_i}$ , respectively.

Based on the velocity analysis derived by Taheri, et al. [14], the separate control of angular velocity of each Mecanum wheel could be determined with respect to the desired  $\mathbf{v}_{X_R}$ ,  $\mathbf{v}_{Y_R}$  and  $\omega_R$ , that is given by Eq. (1) where the parameters of the vehicle are given in Table 4. Rearranging Eq. (1), the Eq. (2) could be derived where the moving speed and angular velocity of the vehicle could be determined by each wheel's angular velocity:

$$\begin{cases} \omega_{1} = \frac{1}{0.1875} (v_{X_{R}} + v_{Y_{R}} + 1.382\omega_{R}), \\ \omega_{2} = \frac{1}{0.1875} (-v_{X_{R}} + v_{Y_{R}} + 1.382\omega_{R}), \\ \omega_{3} = \frac{1}{0.1875} (v_{X_{R}} + v_{Y_{R}} - 1.382\omega_{R}), \\ \omega_{4} = \frac{1}{0.1875} (-v_{X_{R}} + v_{Y_{R}} - 1.382\omega_{R}), \\ \begin{cases} v_{X_{R}} = \frac{3}{64} (\omega_{1} - \omega_{2} + \omega_{3} - \omega_{4}), \\ v_{Y_{R}} = \frac{3}{64} (\omega_{1} + \omega_{2} + \omega_{3} + \omega_{4}), \\ \omega_{R} = \frac{375}{11056} (\omega_{1} + \omega_{2} - \omega_{3} - \omega_{4}). \end{cases}$$

$$(2)$$

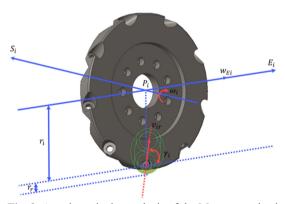


Fig. 9. Angular velocity analysis of the Mecanum wheel

| Table 4. Design parameters in the MWGV |          |           |          |          |
|--|----------|-----------|----------|----------|
| i                                      | 1        | 2         | 3        | 4        |
| $\alpha_i$ (rad)                       | 1        | $\pi - 1$ | $1-\pi$  | -1       |
| $\beta_i$ (rad)                        | $-\pi/2$ | $-\pi/2$  | $-\pi/2$ | $-\pi/2$ |
| $\gamma_i$ (rad)                       | $-\pi/4$ | $\pi/4$   | $-\pi/4$ | $\pi/4$  |
| $l_{ix}$ (m)                           | 0.935    | 0.935     | 0.935    | 0.935    |
| $l_{iy}$ (m)                           | 0.6      | 0.6       | 0.6      | 0.6      |
| $l_i$ (m)                              | 1.111    | 1.111     | 1.111    | 1.111    |
| $r_i$ (m)                              | 0.1875   | 0.1875    | 0.1875   | 0.1875   |

#### 3. Power and mechatronics of the MWGV

To have appropriate selections of the motors, a free-body diagram in Fig. 10 is used to analyze the required power to drive the vehicle. The driving force  $F_d$  should be greater than the sum of rolling friction force  $F_r$ , air drag force  $F_a$ , gravity force along the slope  $F_c$  and inertia force  $F_{ac}$ , which are respectively given in Eqs. (3) to (6):

$$F_r = \mu_r m_T g \cos \theta_s, \tag{3}$$

$$F_a = \frac{1}{2}\rho C_d A_c V_c^2,\tag{4}$$

$$F_c = m_T g \sin \theta_s, \tag{5}$$

$$F_{ac} = m_T a_{ac} (1 + \delta). \tag{6}$$

In Eqs. (3) to (6),  $\mu_r$  is the rolling friction coefficient;  $m_T$  is the total mass of vehicle and payload; g is the gravitational acceleration;  $\theta_s$  is the incline angle of the slope;  $\rho$  is air density;  $C_d$  is drag coefficient;  $A_c$  is the projected frontal area of vehicle;  $V_c$  and  $a_{ac}$  are the velocity and acceleration of the vehicle, respectively;  $\delta$  is the added mass rate, which allows the designer to estimate how much inertia the driving force needs to carry. The required driving force could be computed as:

$$F_d = \frac{T_e i_r \eta_m}{r},\tag{7}$$

where  $T_e$ ,  $i_r$ ,  $\eta_m$  and r stand for the output torque of motor, the reduction ratio, the efficiency of power transmission, and the wheel radius, respectively. Considering the parameters shown in Table 5, the resultant forces were determined and listed in Table 6. The incline angle of the slope was considered to be zero in the general model shown in Fig. 10 to meet the most common factory conditions.

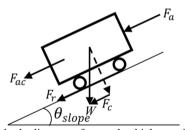


Fig. 10. Free-body diagram of ground vehicle moving on a slope

**Table 5.** Design parameters in the power analysis of MWGV

|                                 | anarybis of 111 ( G )                            |
|---------------------------------|--|
| $m_T$                           | 1480 kg (vehicle weight plus additional payload) |
| g                               | $9.81 \text{ m/s}^2$                             |
| $\mu_r$                         | 0.05   |
| ρ                               | $0.125 \text{ kg/m}^3$                           |
| $C_d$                           | 1.15   |
| $A_c$                           | $1.02 \text{ m}^2$                               |
| $V_c$                           | 1.96 m/s   |
| $\theta_{\scriptscriptstyle S}$ | 0°   |
| $a_{ac}$                        | $0.981 \text{ m/s}^2$                            |
| $\frac{a_{ac}}{\delta}$         | 0.07   |
| $\eta_m$                        | 0.9  |
| r                               | 0.1875 m   |

**Table 6.** Resultant forces of the power analysis

| or the    | oction analysis |
|-----------|-----------------|
| $F_r$     | 725.94 N        |
| $F_a$     | 0.28 N          |
| $F_c$     | 0 N             |
| $F_{ac}$  | 1,553.51 N      |
| $F_d$     | 2,279.73 N      |
| $T_e i_r$ | 474.94 Nm       |

Based on the power analysis, each motor needs to produce a torque of 118.74 Nm. The brushless motor BM-3700E by Adlee Powertronic Company, Ltd. was chosen and connected to a 1:10 reducer MF180X. A rated torque of 119.64 Nm (i.e. one fourth of  $T_e$  times  $i_r$ ) could be produced as the MWGV carries a payload of 740 kg.

Fig. 11 shows the circuit system to power and control the motors. Each motor system requires a driving power of 3700W in 48V. Four 48V30AH rechargeable lithium batteries by Ty-Dynamic Company, Ltd. are connected to the copper ground bars 1 and 2 in parallel. The copper ground bars 1 and 2 are connected to the fuseless breaker with a safety mechanism based on a contactor and an emergency switch (i.e. normal close). The contactor transmits power to the drivers and the motors through the connection of copper ground bar 3. As the emergency switch is pushed, the contactor coil opens the contactor switch and stops providing power to the motors.

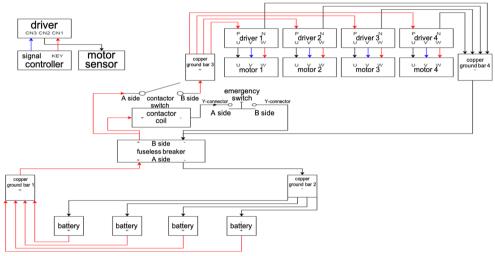


Fig. 11. Circuit system for motor control

## 4. Experimental results

The final assembly of the MWGV could be seen in Fig. 12. A series of speed tests for each motor were executed to ensure the vehicle could be properly controlled. First, each motor was set to speed up to a desired speed (i.e. ranges from 500 to 3000 RPM) in a desired angular acceleration of 250 RPM/s without placing the wheels on the ground. The experimental result of the tested angular acceleration of each motor could be seen in Fig. 13. It was found the proposed axle system could perform the desired acceleration commands properly.

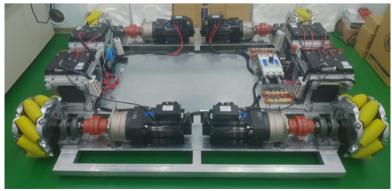


Fig. 12. Final assembly of the MWGV

Next, the MWGV was placed on the ground and perform some moving tests. To test whether each motor could rotate in a desired speed, the vehicle was set to speed up and move left, as shown in Fig. 14. Meanwhile, the motors 1 and 3 speeded up negatively as the motors 2 and 4 speeded up positively, as shown in Fig. 15. The results showed that each motor could speed up as the desired command under the loading conditions.

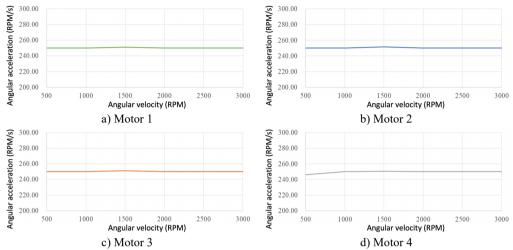
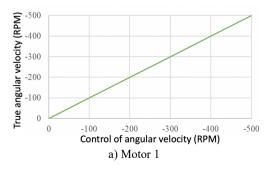
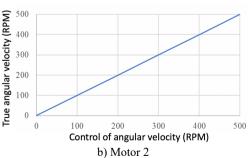


Fig. 13. Average angular acceleration of each motor



a) Initial position b) End position Fig. 14. Demonstration of the transverse movement of the MWGV





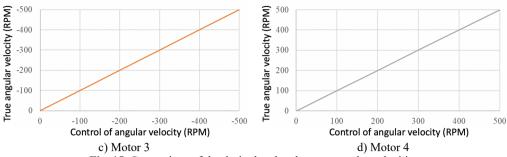


Fig. 15. Comparison of the desired and real motor angular velocities

#### 5. Conclusions

In the field of Industry 4.0 and Smart Manufacturing, linear guideways and AGVs with robot arms above them have been utilized to perform mobile manipulations in the factories. Linear guideway systems were capable for heavier items but the layout was fixed. AGV systems could be more flexible but usually designed for manipulations of weights less than 15 kg. In this paper, a high-payload Mecanum-Wheel Ground Vehicle (MWGV), that was 740 kg in weight, was designed for high-payload mobile manipulation. The proposed design could at least carry 740 kg and the safety factors of the chassis and axle were 1.66 and 6.24, respectively. Each motor produced a rated torque of 119.64 Nm and could accelerate as desired. Currently, the MWGV was successfully completed. The ongoing development of this research team includes the parallel platform above the vehicle and high-payload robot arm with static balancing.

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