

# Method for the extraction of shock signal features based on the upper limit of density integral

Haikun Yang<sup>1</sup>, Hongxia Pan<sup>2</sup>

<sup>1</sup>School of Mechatronics Engineering, North University of China, Taiyuan, China

<sup>2</sup>School of Mechanical and Power Engineering, North University of China, Taiyuan, China

<sup>1</sup>Corresponding author

**E-mail:** <sup>1</sup>yanghaikun1990@foxmail.com, <sup>2</sup>panxh1015@163.com

Received 10 September 2018; received in revised form 13 January 2019; accepted 26 January 2019

DOI <https://doi.org/10.21595/jve.2019.20207>



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**Abstract.** Shock signal features must be extracted for use in pattern recognition or fault diagnosis. In this work, we proposed a method for the feature extraction of shock signals, which are vibration signals that change faster and have larger amplitude ranges than general signals. First, we proposed the concepts of amplitude density for monotonic functions and piecewise monotonic functions. On the basis of these concepts, we then proposed the concept of the upper limit of density integral (ULDI), which was adopted to obtain signal features. Then, we introduced two types of serious fault cracks to the latch sheet of an automatic gun mechanism that is used on warships. Next, we applied the proposed method to extract the features of shock signals from data acquired when the automatic gun mechanism fired with normal and two fault patterns. Finally, we verified the effectiveness of our proposed method by applying the features that it extracted to a support vector machine (SVM). Our proposed method provided good results and was superior to the traditional statistics-based feature extraction method when applied to a SVM for classification. In addition, the former method demonstrated better generalisation than the latter. Thus, our method is an efficient approach for extracting shock signal features in pattern recognition and fault diagnosis.

**Keywords:** signal processing, feature extraction, pattern recognition, fault diagnosis.

## 1. Introduction

Shock signal features must be extracted for utilisation in pattern recognition or fault diagnosis. Methods for the extraction of shock signal features can be classified into two major categories in accordance with the space wherein the signal exists. Methods in the first category involve the direct extraction of the features of an original signal in the time domain; commonly used methods in this category include mathematical statistics, information entropy [1-4]. Methods in the second category involve signal decomposition or transformation followed by feature extraction. Examples of commonly used signal decomposition methods in this category include various filter methods and empirical mode decomposition [5-8]. Commonly applied signal transformation methods include Fourier transform, wavelet transform [9, 10] and Hilbert transform. In fault diagnosis, we first use these methods to obtain the original signal features. Then, we use other methods, such as genetic algorithm [11-14], principal component analysis [15, 16] and kernel principal component analysis [17, 18] to perform necessary selections and transformations to obtain the appropriate features.

Many scholars have improved the classical algorithms for signal feature extraction. Yang and Nataliani [19] presented a novel method for improving fuzzy clustering algorithms that can automatically compute individual feature weight and simultaneously reduce irrelevant feature components. They first considered the objective function of fuzzy c-means with feature-weighted entropy, constructed a learning schema for parameters and then reduced irrelevant feature components. Saif et al. [20] proposed the application of the nonlinear complete ensemble empirical mode decomposition method with adaptive white noise to decompose signals into intrinsic mode functions (IMFs). Deng et al. [21] revealed the inherent characteristics of vibration signals by calculating the fuzzy information entropy values of IMFs and considering them as feature vectors. They then proposed an improved particle swarm optimisation (PSO) algorithm by

using the diversity mutation, neighbourhood mutation, learning factor and inertia weight strategies for the basic PSO. Finally, they used the improved PSO algorithm to optimise the parameters of least squares support vector machines (LS-SVM) for the construction of an optimal LS-SVM classifier. Zhao et al. [22] proposed an enhanced empirical wavelet transform (MSCEWT) based on the maximum-minimum length curve method. The proposed MSCEWT can obtain fewer IMFs than empirical mode decomposition and ensemble empirical mode decomposition.

Original features affect the accuracy of pattern recognition and fault diagnosis, and additional signal properties can be fully reflected by increasing the number of features. The features that can represent the main properties of signals with different properties may vary. Therefore, developing a new method for signal feature extraction is crucial. In this work, we proposed a method for extracting shock signal features. We first proposed the concept of the amplitude density of a signal. Then, we proposed the concept of the ULDI, which is adopted for signal feature extraction. Finally, we analysed the features of shock signals for an automatic gun mechanism to verify the effectiveness of our proposed method.

## 2. Amplitude density and density integral

### 2.1. Amplitude density for monotonic functions

Assume that a signal  $f(t)$  is defined in the interval  $[a, b]$  and satisfies  $f'(t) \geq 0, t \in [a, b]$  where  $A = \min\{f(t)|t \in [a, b]\}$ ,  $B = \max\{f(t)|t \in [a, b]\}$ . The functional image of  $f(t)$  is presented in Fig. 1.

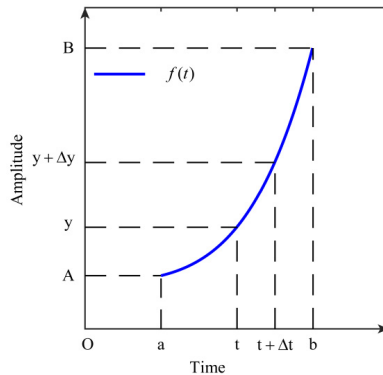


Fig. 1. Functional image of  $f(t)$

Then, Eq. (1) is established by considering points  $[t, y]$  and  $(t + \Delta t, y + \Delta y)$  in  $f(t)$ :

$$\Delta t = f^{-1}(y + \Delta y) - f^{-1}(y). \tag{1}$$

We define a function  $r(y)$  that satisfies Eq. (2):

$$\int_y^{y+\Delta y} r(x) dx = \frac{\Delta t}{b - a}. \tag{2}$$

Both ends of Eq. (2) are divided by  $\Delta y$ . The limit is taken as Eq. (3). Then, Eq. (3) becomes equal to Eq. (4):

$$\lim_{\Delta y \rightarrow 0} \frac{\int_y^{y+\Delta y} r(x) dx}{\Delta y} = \lim_{\Delta y \rightarrow 0} \frac{\Delta t}{(b - a)\Delta y}, \tag{3}$$

$$r(y) = \frac{1}{b-a} (f^{-1})'(y). \tag{4}$$

$r(y)$  is defined as the amplitude density function of  $f(t)$  in the interval  $[a, b]$ .  $r(y)$  reflects the probability of  $y$  that  $f(t)$  takes in the interval  $[a, b]$ .  $r(y) \geq 0$  exists, and Eq. (5) is true. The opposite number of the right end in Eq. (4) when  $f'(t) \leq 0$  is taken. Eq. (6) is thus established:

$$\int_A^B r(y) dy = 1, \tag{5}$$

$$r(y) = \frac{1}{b-a} |(f^{-1})'(y)|. \tag{6}$$

### 2.2. Amplitude density for piecewise monotonic functions

Assume that a signal  $f(t)$  that is defined in the interval  $[a, b]$  can be divided into amounts of monotonic intervals and the derived function  $f'(t)$ ,  $t \in [a, b]$  exists where:

$$A = \min\{f(t)|t \in [a, b]\}, B = \max\{f(t)|t \in [a, b]\}.$$

The functional image of  $f(t)$  is illustrated in Fig. 2. The piecewise function in every monotonic interval is assumed to be expressed as  $f_i(t)$ ,  $i = 1, 2, \dots, n$ .

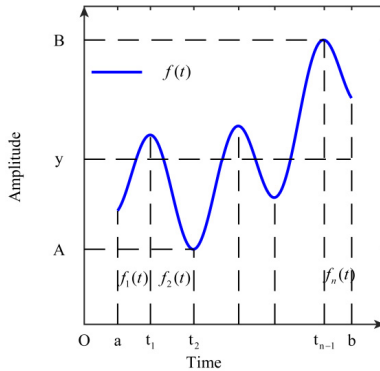


Fig. 2. Function  $f(t)$  that is defined in finite monotonic intervals

Considering the amplitude density of  $f(t) = y$ , the piecewise function  $f_k(t)$ ,  $k \in C$  and  $C \subseteq \{1, 2, \dots, n\}$  is assumed to take the value  $y$ . On the basis of our analysis in section 2.1, we show that the amplitude density  $r(y)$ , where  $f(t) = y$ , should be established as (7):

$$r(y) = \sum_{k \in C} \frac{1}{b-a} |(f_k^{-1})'(y)|. \tag{7}$$

The interval of the definition of the piecewise inverse function  $f_i^{-1}(y)$ ,  $i = 1, 2, \dots, n$ , is extended. The result of the extension is plotted in Fig. 3. For every extreme point or end point in  $f(t)$ , the minimum points are extended to  $y = A$ , and the maximum points are extended to  $y = B$ . The piecewise inverse function that has been extended is still expressed as  $f_i^{-1}(y)$ ,  $y \in [A, B]$ ,  $i = 1, 2, \dots, n$  to facilitate expression in this paper. Therefore, Eq. (7) is equal to Eq. (8). We can still consider  $r(y)$  as the amplitude density function of  $f(t)$ :

$$r(y) = \frac{1}{b-a} \sum_{i=1}^n |(f_i^{-1})'(y)|. \tag{8}$$

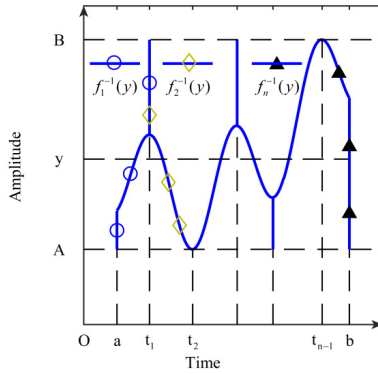


Fig. 3. Extended piecewise inverse functions

### 2.3. ULDI

Both ends of Eq. (8) are subjected twice to the definite integral operation in the interval  $[A, y_2]$  and  $[A, y]$ ,  $y_2 \in [A, B]$ , of which the result is Eq. (9):

$$\int_A^y \int_A^{y_2} r(y_1) dy_1 dy_2 = \int_A^y \int_A^{y_2} \sum_{i=1}^n \frac{1}{b-a} |(f_i^{-1})'(y_1)| dy_1 dy_2, \quad (9)$$

let:

$$\Phi(y) = \int_A^y \int_A^{y_2} r(y_1) dy_1 dy_2,$$

then, Eq. (9) is equal to Eq. (10):

$$\begin{aligned} \Phi(y) &= \int_A^y \int_A^{y_2} \sum_{i=1}^n \frac{1}{b-a} |(f_i^{-1})'(y_1)| dy_1 dy_2 \\ &= \frac{1}{b-a} \int_A^y \sum_{i=1}^n |f_i^{-1}(y_2) - f_i^{-1}(A)| dy_2 = \frac{1}{b-a} \sum_{i=1}^n \int_A^y |f_i^{-1}(y_2) - f_i^{-1}(A)| dy_2. \end{aligned} \quad (10)$$

We can ignore the influence of inverse functions without differential coefficients at the extreme points or end points of  $f(t)$  when we calculate Eq. (10). Therefore, the value of  $f_i^{-1}(y)$ ,  $y \in [A, B]$  and  $i = 1, 2, \dots, n$  at the local area of these points is readjusted to ensure that  $(f_i^{-1})'(y)$  exists, whereas the value of  $\Phi(y)$  remains unchanged. We can handle this operation in this manner because the value of the integral is unchanged by standard integration and changing the integrand on a set of zero measure does not change the value of the integral (measure theory).

The area of the shaded regions in Fig. 4 is regarded as  $S(y)$ . Eq. (11) is true. Furthermore, we regard the curve in Fig. 5 as  $P_y(t)$ , which is formed by  $f(t)$  and the constant:

$$S(y) = \sum_{i=1}^n \int_A^y |f_i^{-1}(x) - f_i^{-1}(A)| dx. \quad (11)$$

$P_y(t)$  is easily obtained when  $y$  is determined. On the other hand,  $S(y)$  can be expressed as Eq. (12):

$$S(y) = (b-a)(y-A) - \int_a^b [P_y(t) - A] dt. \quad (12)$$

We can obtain Eq. (13) by combining Eqs. (10), (11) and (12). Then, Eqs. (14) and (15) are true:

$$\Phi(y) = y - \frac{1}{b-a} \int_a^b P_y(t) dt, \quad (13)$$

$$\Phi'(y) = 1 - \frac{d}{(b-a)dy} \int_a^b P_y(t) dt, \quad (14)$$

$$r(y) = \frac{d^2}{(a-b)dy^2} \int_a^b P_y(t) dt. \quad (15)$$

$\Phi(y)$ ,  $\Phi'(y)$  and  $r(y)$  are uniquely determined by each other when  $f(t)$  is determined. We designate  $\Phi'(y)$  as the ULDI of a signal. The data obtained in engineering applications are discrete. The error of the first-order differential operation is low in the calculation of the differential operation of Eq. (14). When solving the second-order differential operation in Eq. (15), the local of the first-order differential section steps into a jump. The second-order differential is therefore not consistent with the actual value if the differential region is small. On the other hand, if the differential region is large, the accuracy of the calculation will decrease. Signal features will be extracted by utilising Eq. (14) to avoid this problem.

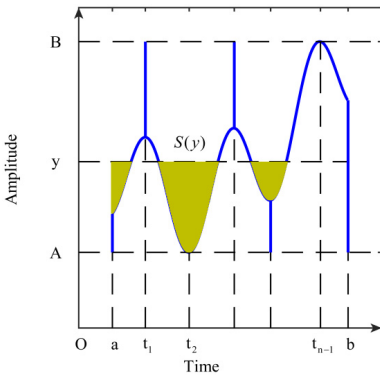


Fig. 4. Area  $S(y)$  of the shaded regions

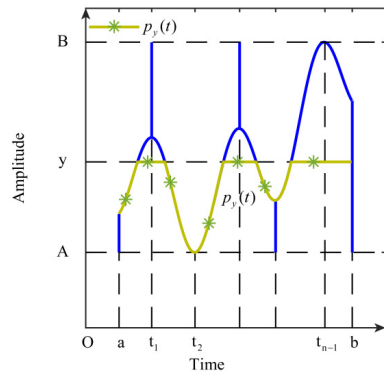


Fig. 5. Curve of  $P_y(t)$

### 3. Features of shock signals

As discussed in this section, we introduced two types of serious fault cracks to the latch sheet of an automatic gun mechanism that is used on warships. Then, we applied the proposed method to extract the features of shock signals from data acquired when the automatic gun mechanism fired with normal and two fault patterns. The firing frequency of the automatic gun mechanism is 10 Hz. The main parameters of the sensors that we used in this work are shown in Table 1.

Table 1. Sensor parameters

Performance	Value
Sensitivity	1.0 mV/g ( $\pm 15\%$ )
Measurement range	$\pm 5,000$ g pk
Frequency range	0.4 Hz to 7,500 Hz ( $\pm 10\%$ )
Electrical filter cutoff frequency	$\geq 7.5$ kHz ( $-10\%$ )
Resonant frequency	$\geq 50$ kHz
Broadband resolution	0.02 g rms (1kHz to 10 kHz)

We set the sampling frequency as the maximum sampling frequency (204.8 kHz) of the signal collector to obtain additional details in the time domain and the sampling time as 5 s. The

environmental parameters of the experiment are shown in Fig. 6. The main measuring point and the two types of serious fault cracks are illustrated in Fig. 7.

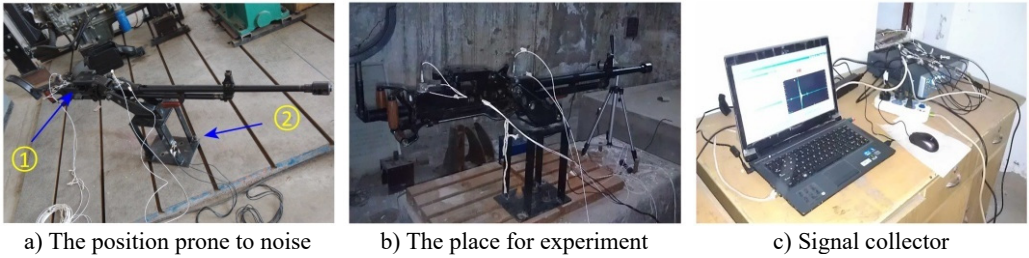


Fig. 6. Environment of the experiment



Fig. 7. Main measuring point and two types of serious fault cracks

### 3.1. ULDI of shock signals

Only the actual effective time period of the original signal is intercepted for analysis to avoid the interference of invalid signals with effective signals. The shock signals in the time domain are plotted in Fig. 8. The ULDI of each signal are shown in Fig. 9. The area  $[-1000, 0] \times [0, 0.3]$  of Fig. 9 is presented in Fig. 10 to properly illustrate the ULDI of each signal. From Fig. 10, we can conclude that under the same density integral, the amplitudes that correspond to different working modes are different.

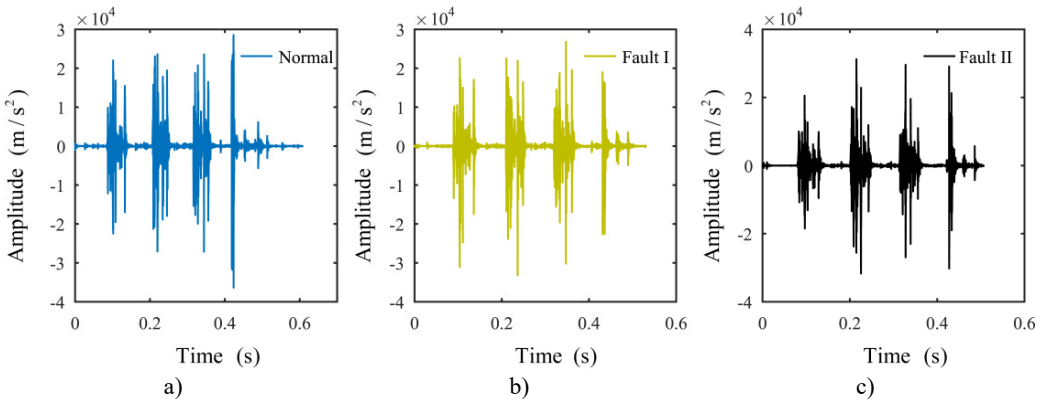


Fig. 8. Signals in the time domain

### 3.2. Signal features

For a continuous shock signal  $f(t)$ , the ULDI  $\Phi'(y)$  is a strictly monotonically increasing function of  $y$ . Therefore, for a determined value of  $\Phi'(y)$ , we can obtain the amplitude  $y$  that corresponds to  $\Phi'(y)$  through bisection, which is a method that is commonly used to identify zero

points. The amplitude that corresponds to a determined value of  $(\Phi_{i,j}^m)'(y)$  can be denoted as  $y_{i,j}^m$ ,  $m \in \{1,2,3\}$ ,  $i \in \{1,2,3,\dots\}$ ,  $j \in \{1,2,3,\dots\}$ , where  $m$  means the index of signals generated by different patterns,  $i$  means the index of signals generated by same pattern and  $j$  means the index of amplitudes that correspond a signal.

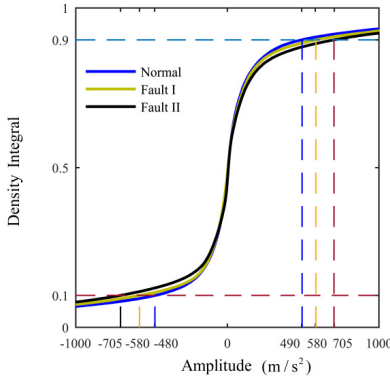


Fig. 9. Density integrals of signals

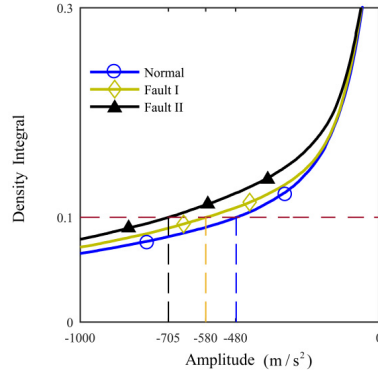


Fig. 10. Area  $[-1000,0] \times [0,0.3]$  of Fig. 9

Three signals that correspond to the different firing pattern with respect to the different values of  $\Phi'(y)$  are shown in Table 2, which means  $m \in \{1,2,3\}$ ,  $i \in \{1\}$ ,  $j \in \{1,2,\dots,8\}$  and  $\Phi'(y) \in \{0.1,0.2,\dots,0.8\}$ . Therefore, we can consider  $F_i^m = (y_{i,1}^m, y_{i,2}^m, \dots, y_{i,N}^m)^T$ ,  $N = 8$ , as the feature of a signal. From Table 2, we can infer that the difference between the different work patterns first decreases and then increases as the density integral increases. This behaviour reflects the similarities and differences between each firing pattern.

Table 2. Signal features

Density integral		0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8
Amplitude (m/s <sup>2</sup> )	Normal	-478.13	-138.11	-62.67	-23.41	1.24	24.53	64.67	151.75
	Fault I	-579.77	-149.66	-65.09	-25.29	-0.02	25.03	70.32	161.02
	Fault II	-704.80	-185.57	-65.76	-17.61	1.37	24.90	77.01	180.88

### 3.3. Applying extracted features to a SVM

We further verified the effect of our proposed method and selected the data from one sensor for verification (there are 8 sensors in the actual test of sampling signals). We sampled 14 effective groups of data that correspond to each work pattern for application into an SVM, and limited by the service life of the automatic gun mechanism. Only small samples can be sampled. The steps of feature extraction and verification are as follows.

Step 1: on the base of original signals, intercept the signal segment when the latch sheet is working.

Step 2: the instantaneous frequency function of IMF2 is obtained by EMD decomposition of the signal that is intercepted.

Step 3: on the base of instantaneous frequency function of IMF2, we extracted the features that are similar to the features presented in Section 3.2.

Above what we analysed, there are 42 samples (features) for classification. At the process of training and testing SVM, we chose to leave one out cross validation. The results of the training are presented in Table 3, and the results of testing are provided in Table 4 [23-25].

The dimensionality of the features  $F_i^m = (y_{i,1}^m, y_{i,2}^m, \dots, y_{i,N}^m)^T$  used for the SVM is 11, and  $\Phi'(y) \in \{0.1,0.15,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.85,0.9\}$ ,  $i \in \{1,2,\dots,42\}$ ,  $j \in \{1,2,\dots,11\}$ ,  $N = 11$ . We selected the radial basis function (RBF) as the kernel of the SVM. The kernel is

expressed as:

$$K(x, y) = \exp\left(-\frac{\|x - y\|^2}{2\sigma^2}\right).$$

$\sigma > 0$ , of which  $\sigma$  is the width and was selected as 5.

We validated the effectiveness of the proposed method by comparing its performance with that of a statistics-based method. We selected the same sample data and SVM parameters for classification. In general, we can represent the instantaneous frequency data that correspond to a shock signal as  $\{x_1, x_2, \dots, x_N\}$ . Table 5 shows the representation of each component of the feature extracted from signals on the basis of mathematical statistics. We can regard this feature as  $(\bar{x}, x_p, x_{rms}, x_r, K, C, I, S)^T$ . The dimensionality of the features is 8. Training results are shown in Table 6, and testing results are shown in Table 7.

From Tables 3 and 4, we can infer that the SVM conflates features that correspond to normal patterns with those that correspond to fault I patterns. Although the classification results are acceptable, accuracy must be improved by combining other types of features. As inferred from Tables 4 and 7, the classification performance of the proposed method is superior to that of the traditional method that constructs features on the basis of mathematical statistics. Tables 3, 4, 6 and 7 show that the generalisation of the former method is better than that of the latter method.

**Table 3.** Results of SVM training

Training	Normal	Fault I	Fault II
Normal	13	0	0
Fault I	1	14	1
Fault II	0	0	13
Accuracy (%)	92.85	100	92.85

**Table 4.** Results of SVM testing

Test	Normal	Fault I	Fault II
Normal	12	1	0
Fault I	2	12	1
Fault II	0	1	13
Accuracy (%)	85.71	85.71	92.85

**Table 5.** Feature representation

Feature components	Representation	Feature components	Representation
Absolute mean	$\bar{x} = \frac{1}{N} \sum_{i=1}^N  x_i $	Wave form	$K = \frac{x_{rms}}{\bar{x}}$
Peak value	$x_p = \max  x_i $	Peak index	$C = \frac{x_p}{x_{rms}}$
Mean square	$x_{rms} = \sqrt{\frac{1}{N} \sum_{i=1}^N x_i^2}$	Impulse index	$I = \frac{x_p}{\bar{x}}$
Root square	$x_r = \left(\frac{1}{N} \sqrt{\sum_{i=1}^N  x_i }\right)^2$	Skewness	$S = E \left[ \left( \frac{x - E(x)}{\sqrt{D(x)}} \right)^3 \right]$

**Table 6.** Training results for the features constructed on the basis of mathematical statistics

Training	Normal	Fault I	Fault II
Normal	12	0	0
Fault I	2	13	1
Fault II	0	1	13
Accuracy (%)	85.71	92.85	92.85

**Table 7.** Testing results for features constructed on the basis of mathematical statistics

Test	Normal	Fault I	Fault II
Normal	12	1	1
Fault I	2	11	0
Fault II	0	2	13
Accuracy (%)	85.71	78.57	92.85



## 4. Conclusions

We proposed a method for extracting shock signal features. The proposed method has low computational cost. Given this characteristic, our proposed method can be used as a simple and efficient tool for the extraction of shock signal features for pattern recognition or fault diagnosis. Using the features extracted by our proposed method in pattern recognition yielded good results. Nevertheless, other types of features must be combined to improve identification accuracy.

The shock signals used in this work are deterministic signals, which are repeatable. Thus, the proposed method can reliably and robustly differentiate different signal types. However, this method is not necessarily applicable to signals that are corrupted and is sensitive to the time domain partition. Signals in the time domain must be first partitioned prior to the application of the proposed method to avoid these problems.

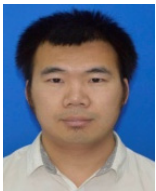
## Acknowledgements

The authors gratefully acknowledge the support from the National Natural Science Foundation of China (Grants 51675491 and 51175480).

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**Haikun Yang** was born in Enshi, Hubei Province, China. He received his B.E. degree from Hubei University for Nationalities, Enshi, China, in 2014, and now is a Ph.D. student in the School of Mechatronics Engineering, North University of China, Taiyuan, China. His interests include signal processing, artificial intelligence and philosophical theory.



**Hongxia Pan** received the M.Sc. degree in mechanical engineering from Nanjing University of Science and Technology, Nanjing, China, in 1981. Now he works at North University of China. His current research interests include system identification, signal processing, and fault diagnosis. Because of his continuous important contribution to these fields, he has been awarded the special allowance of the State Council since 1992, which is a honor for a few excellent scientific researchers in China.