2465. Optimal design of the main support structure of space camera aiming at the RMS value of random response

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Abstract. To explore the optimal design method for main support structure of micro satellite, this paper proposed a method targeting the random acceleration response RMS value of the space camera installation position when design the main support structure of LQ-video satellite in Jilin-1 group satellites. Camera main support structure optimization mathematical model was established, and the thickness and flexible beam position of the flexible beam support structure has been optimized in the establishment of the optimization mathematical model. When the flexible beam thickness is 2.5 mm, and the distance between it and the support structure mounting surface is 94.5 mm, the camera installation point acceleration response root mean square (RMS) value is minimal. Engineering analysis showed that the maximal random response RMS of the camera installation point is 19.6 grms and the maximal relative magnification is 0.93. The camera mechanics test showed that the maximal relative error of finite element analysis and experimental measurements is 4.0 % and the maximal relative magnification of the response is 1.2 which is less than the overall index 1.5. It proved that the optimization method is effective and feasible.

Keywords: micro satellite, random vibration, space camera, main support structure, optimal design.

Nomenclature

- M *n*-order mass matrix
- **C** Damping matrix
- K Stiffness matrix
- ܆ Displacement vector
- \dot{X} Velocity vector
- \ddot{x} Acceleration vector
- $f(t)$ System incentives
- $\ddot{Y}(t)$ The acceleration incentive
- $S_{\ddot{Y}}(w)$ Power spectral density of acceleration incentive
- E Acceleration vector
- W_i System n -degree natural frequency
- x_i Mode of vibration
- ϕ_i Mass normalized vibration mode
- ξ_i ξ_i System *i*th modal damping ratio
 Y_i ith mode participation coefficien
- ith mode participation coefficient
- u_i u_i ith modal displacement
 $h_i(\tau)$ ith impulse response fun
- ith impulse response function
- \ddot{R}_Y Input auto correlation function
- $H_i(w)$ Frequency transfer function
- $h_i(t)$ Impulse response function
- λ_i λ_i ith isolated eigen values
{ φ_i } Mode vectors
- Mode vectors
- $\lambda_{i,j}$ Derivative of λ_i under the design variable t_j $(j = 1, 2, ..., L)$
- $\{\varphi_{i,j}\}\$ Derivative $\{\varphi_i\}$ under the design variable t_j $(j = 1, 2, ..., L)$
- $[K_i]$ Derivative matrix of $[K]$ under the design variable t_i
- $[M_i]$ Derivative matrix of $[M]$ under the design variable t_i
- t_{o} Thickness of flexible joint
- h_e Distance from flexible beam to support structure mounting surface
- t_i Thickness variable
- h_i Distance variable

1. Introduction

Modern micro-satellite has a strong practicability for small size, light weight, low cost, short development cycle and high performance characteristics [1, 2]. Therefore, the micro satellite has been paid more attention in the field of international space technology. With the vigorous development of micro satellite, the effective load ratio is increasing, and the requirements of the main structure of the satellite are more severe [3-5]. Exploring optimization method is even more urgent for main structure design of micro satellite.

LQ-video satellite in Jilin-1 group satellites is a micro video imaging satellite whose mass is no more than 95 Kg. Aiming at reducing the satellite structure mass and volume, it uses space-borne integration design to improve the structure density of micro satellite. The camera is connected with the satellite through the camera main support structure. When the rocket launches, the satellite suffering random acceleration vibration excitation which is integrated by pulsation generation rocket thrust, jet noise and turbulent boundary layer noise [6-8]. If the acceleration vibration directly passed through the main support structure to the camera, it will cause the camera structural deformation or even destroyed. Therefore, the camera main support structure should be optimized to gain a better dynamic performance under a given frequency band.

The existing research, based on random vibration theory and test, mostly examined the structural strength of the satellite rather than optimized the structure of the dynamic parameters [9-12]. For instances, W. Jung, A. P. Mazzoleni, J. Chung [13] presents a dynamic analysis of a tethered satellite system with a moving mass.The analysis results show that a one-piece dumbbell model is qualitatively valid for studying the system under certain conditions, such as when the initial liberation angles, moving mass velocity, and moving mass size are small, the tether length is large, and the mass ratio of the two satellites is large. You B., Zhang H., Li W., et al. [14] presented a methodology for modeling and analysis of satellite antenna systems considering the effects of the joint clearance and reflector flexibility in the system. Based on a thorough geometric description of the eccentricity vector, the multibody dynamics of satellite antenna are analyzed by considering a flexible reflector with ideal and nonideal joints.

According to LQ-video satellite overall design requirements, this paper proposed a method to optimize design camera main support structure targeting the random vibration response RMS value of the camera installation position, and established a random vibration response optimization model. The thickness of the flexible joint and flexible beam position has been optimized. In order to verify the optimization results, engineering analysis and mechanical testing of the optimized camera main support structure are carried out. The results showed that the optimization designed main support structure match the overall satellite design specifications well, and the optimize design method is effective and feasible.

2. Optimization model

Size optimization is one of the most important topology optimization method, especially used

in structure optimization [15-17]. It refers to a mathematical method for optimizing material distribution in a given area under a given load conditions, constraints and performance indicators. The optimization mathematical is established from the objective function, design variables and constraint conditions, and the optimization process is explained in this section.

2.1. Systematic random response function

Spectrum analysis method is generally used in the random response. An n degrees' freedom linear system is expressed by random excitation and its kinetic equation [18, 19] is represented as Eq. (1):

$$
\mathbf{M}\ddot{\mathbf{X}} + \mathbf{C}\dot{\mathbf{X}} + \mathbf{K}\mathbf{X} = f(t),\tag{1}
$$

where, M , C and K respectively represent *n*-order mass matrix, damping matrix and stiffness matrix. **X** is displacement vector, $\dot{\mathbf{X}}$ is velocity vector, $\ddot{\mathbf{X}}$ is acceleration vector and $f(t)$ is system incentives.

Assume the acceleration incentive is $\ddot{Y}(t)$, and its power spectral density (PSD) is $S_{\ddot{Y}}(w)$, the kinetic random vibration equation is represented as Eq. (2):

$$
M\ddot{X} + C\dot{X} + KX = ME\ddot{Y}(t),
$$
\n(2)

where, **E** indicates an acceleration vector.

First, to solve system's intrinsic mode, it should be $C=0, f(t)=0$ and the system free motion equation [20] is represented as Eq. (3):

$$
M\ddot{X} + KX = 0. \tag{3}
$$

The corresponding characteristic equation is represented as Eq. (4):

$$
\mathbf{K} - w^2 \mathbf{M} = 0. \tag{4}
$$

System *n*-degree natural frequency is w_i , and the corresponding mode of vibration is x_i , $i = 1, 2,..., n$. where, $m_i = x_i^T M x_i$, $k_i = x_i^T k x_i$, $w_i^2 = k_i / m_i$, the mode of vibration x_i multiplies a constant multiplier and the mass normalized vibration mode is ϕ_i . In classical damping, the Eq. (2) rewrite as follows:

$$
\ddot{u}_i + 2w_i \xi_i \dot{u}_i + w_i^2 u_i = \Upsilon_i \ddot{Y}(t), \quad (i = 1, 2, \dots, n). \tag{5}
$$

In this formula, ξ_i is the system *i*-th modal damping ratio; Y_i is the *i*-th mode participation coefficient:

$$
\Upsilon_i = \phi^T \mathbf{M} \mathbf{E}.\tag{6}
$$

Relationship between $X(t)$ and u_i is:

$$
\mathbf{X}(t) = \begin{bmatrix} \phi_1 & \phi_2 & \cdots & \phi_n \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ \vdots \\ u_1 \end{bmatrix} = \Phi u(t) = \sum_{i=1}^n u_i \phi_i.
$$
 (7)

Solution of Eq. (5) in the time domains is:

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$$
u_i = \Upsilon_i \int_{-\infty}^{+\infty} h_i(\tau) \, \dot{Y}(t-\tau) d\tau,\tag{8}
$$

where, $h_i(\tau)$ is the *i*-th impulse response function.

Through Eqs. $(7)-(8)$, we get:

$$
X(t) = \sum_{i=1}^{n} Y_i \phi_i \int_{-\infty}^{+\infty} h_i(\tau) \ddot{Y}(t-\tau) d\tau.
$$
 (9)

The auto correlation function of the matrix $X(t)$ is:

$$
R_{XX}(\tau) = \mathbf{E}[X(\tau)X^{T}(t+\tau)]
$$

\n
$$
= \sum_{i=1}^{n} \sum_{j=1}^{n} Y_{i}Y_{j}\phi_{i} \phi_{i}^{T} \cdot \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \mathbf{E}[\ddot{Y}(t-\tau_{1})\ddot{Y}(t-\tau_{2}+\tau)] h(\tau_{1})h(\tau_{2})d\tau_{1}d\tau_{2}
$$

\n
$$
= \sum_{i=1}^{n} \sum_{j=1}^{n} Y_{i}Y_{j}\phi_{i} \phi_{i}^{T} \cdot \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} \ddot{R}_{Y}(\tau+\tau_{1}-\tau_{2})h(\tau_{1}) h(\tau_{2})d\tau_{1}d\tau_{2}.
$$
\n(10)

According to the Wiener-Khintchine relationship [21], output PSD is the Fourier transform of the output of autocorrelation function. By exchanging integral order, and introducing variable $\theta = t + \tau_1 - \tau_2$, we get output PSD function as follows:

$$
S_{XX}(w) = \sum_{i=1}^{n} \sum_{j=1}^{n} \gamma_i \gamma_j \phi_i \phi_i^T h_i(\tau_1) e^{i w \tau_1} h_j(\tau_2) e^{-i w \tau_2} \cdot \left[\frac{1}{2\pi} \int_{-\infty}^{+\infty} \ddot{R}_Y(\theta) e^{-i w \theta} d\theta \right] d\tau_1 d\tau_2.
$$
 (11)

Input PSD function \ddot{S}_Y is the \ddot{S}_Y Fourier transform of input auto correlation function \ddot{R}_Y , and frequency transfer function $H_i(w)$ is the Fourier transform of impulse response function $h_i(t)$, then Eq. (11) rewrite as Eq. (12) :

$$
S_{XX}(w) = \sum_{i=1}^{n} \sum_{j=1}^{n} Y_i Y_j \phi_i \phi_i^T H_i(w) H_j(w) \ddot{S}_Y(w).
$$
 (12)

Generally, ignoring the cross-order terms to simplify approximation method is used in engineering in Eq. (12), the response PSD abbreviated as follows:

$$
S_{XX}(w) = \sum_{i=1}^{n} Y_i^2 \phi_i \phi_i^T |H_i(w)|^2 \ddot{S}_Y(w).
$$
\n(13)

The random acceleration RMS response expression which is also the optimization objective function shown in Eq. (14):

$$
\sigma_{XX}^2 = \int_{-\infty}^{+\infty} S_{XX}(w) dw = \sum_{i=1}^n Y_i^2 \phi_i \phi_i^T \int_{-\infty}^{+\infty} |H_i(w)|^2 \ddot{S}_Y(w) \, dw. \tag{14}
$$

2.2. System sensitivity

Modal analysis is used to determine the vibration characteristics of the structure. It is mainly about the natural frequency and vibration mode of the system structure, which is an important 2465. OPTIMAL DESIGN OF THE MAIN SUPPORT STRUCTURE OF SPACE CAMERA AIMING AT THE RMS VALUE OF RANDOM RESPONSE. LIN LI, LUYANG TAN, DONG WANG, HONGBO YANG

index to investigate the dynamic stiffness. Structural low order mode is also an important basis for modifying the structure. The modal sensitivity of the structure is analyzed as follows.

 λ_i and $\{\varphi_i\}$ are the *i*-th isolated eigen values and the corresponding mode vectors, which satisfy the characteristic Eq. (15):

$$
([\mathbf{K}] - \lambda_i [\mathbf{M}] \{ \varphi_i \} = 0. \tag{15}
$$

 $\lambda_{i,j}$ and $\{\varphi_{i,j}\}\$ are the derivative of λ_i and $\{\varphi_i\}\$ under the design variable t_j $(j = 1, 2, ..., L)$, $[K_{i,j}]$ and $[M_{i,j}]$ are the derivative matrix of $[K]$ and $[M]$ under the design variable t_i . Eigen values sensitivity $\lambda_{i,j}$ and modal vector sensitivity $\{\varphi_{i,j}\}$ are as follow:

$$
\lambda_{i,j} = {\varphi_i}_n^T ([\mathbf{K}_{,j}] - \lambda_i [\mathbf{M}_{,j}]) {\varphi_i} {\varphi_{i,j}},
$$
\n(16)

$$
\{\varphi_{i,j}\} = \sum_{\substack{k=1 \ k \neq i}}^{\infty} \frac{1}{\lambda_i - \lambda_k} \left(\{\varphi_k\}^T \left([\mathbf{K}_{,j}] - \lambda_i [\mathbf{M}_{,j}] \right) \bullet \{\varphi_i\} \right) \ - \frac{1}{2} \left(\{\varphi_i\}^T \left[\mathbf{M}_{,j} \right] \{\varphi_i\} \right) \{\varphi_i\}.
$$

To calculate $\lambda_{i,j}$ and $\{\varphi_{i,j}\}\$, it should be calculate $[\mathbf{K}_{,j}] = \frac{\partial[\mathbf{K}]}{\partial t_j} = \sum \frac{\partial[\mathbf{K}]}{\partial t_j}$ and $[\mathbf{M}_{i,j}] = \frac{\partial[\mathbf{M}]}{\partial t_i} = \sum \frac{\partial[\mathbf{M}]}{\partial t_i}$ first. In this paper, shell thickness t is used in the optimization analysis. Therefore, the derivative matrix of the shell element matrix C and the derivative matrix of the mass matrix D are given.

$$
\frac{\partial [\mathbf{K}]^e}{\partial t_j} = \frac{[\mathbf{K}]^e}{t_j},
$$
\n
$$
\frac{\partial [\mathbf{M}]^e}{\partial t_j} = \frac{[\mathbf{M}]^e}{t_j}.
$$
\n(18)

Derivative Eq.
$$
(14)
$$
, we would get random acceleration response sensitivity.

2.3. Design variables

Support structure flexible beam thickness T and distance from flexible beam to support structure mounting surface H are written as Eq. (20):

$$
\mathbf{T}' = (t_1, t_2, t_3, \dots t_e, \dots t_n)^T, \quad \mathbf{H}' = (h_1, h_2, h_3, \dots h_e, \dots h_n)^T,
$$
\n(20)

where, t_e is thickness of flexible joint, h_e is distance from flexible beam to support structure mounting surface.

2.4. Mathematical model

LQ-video satellite requires that the primary frequency of the camera main support structure is greater than the camera primary frequency 110 Hz. The safety factor is 1.2, the primary frequency of the camera main support structure is no less than 132 Hz. The t_e and h_e satisfy the Eq. (21):

$$
1 \le t_i \le t_e \le 5,
$$

\n
$$
6.5 \le h_i \le h_e \le 105.5,
$$
\n(21)

where, t_i represents the thickness variable, h_i represents the distance variable.

The camera main support structure size optimization mathematical model is expressed as Eq. (22):

find:
$$
\mathbf{T}' = (t_1, t_2, \dots, t_e, \dots, t_n)^T,
$$

\n
$$
\mathbf{H}' = (h_1, h_2, h_3, \dots, h_e, \dots, h_n)^T,
$$

\nMinimize: $C(x) = \sigma_{xx}^2$,
\nSubject to: $f_1 \ge 132$,
\n $1 \le t_i \le t_e \le 5$,
\n $6.5 \le h_i \le h_e \le 105.5$.

Until now, the random vibration mean square response is converted into a deterministic harmonic response analysis problem based on the virtual excitation method, and the sensitivity of the modal sensitivity and random acceleration response are analyzed.

3. Optimization process and results

According to the mathematical model in Section 2, the sizing optimization was introduced to optimize the thickness of the flex joint and the flex joint position in the main support structure of the camera. The optimization design flow is shown in Fig. 1.

Fig. 1. Flow chart

Frequency (Hz)	Power spectral density		
20-150	$+3$ dB/oct		
150-280	0.08 g ² /Hz		
280-320	0.30 g ² /Hz		
320-380	0.20 g ² /Hz		
380-850	0.10 g ² /Hz		
850-1000	0.04 g ² /Hz		
1000-2000	0.01 g ² /Hz		

Table 1. The acceleration power spectrum (PSD)

Overall design of the LQ-video satellite requires that the height of main support structure of the camera is 118 mm. The material of the main supporting structure is Titanium alloy TC4 which is provided with low density and high strength.

The applied loads are the random acceleration which is from the rocket in launching. The acceleration power spectrum is shown in Table 1, and the RMS value of PSD is 10.16 g. Structural damping is 0.03 in this model.

Optimize step size is 0.5 mm during the optimization design process. After 69 steps of iteration, the random vibration acceleration response of the camera mounting point is minimal and thickness of flexible joint t_e is 2.5 mm, distance h_e is 94.5 mm. Optimization iterative process convergence curve is shown in Fig. 2.

4. Finite element numerical analysis

To estimate the optimization result, the finite element analysis is carried out by using MSC. Patran&Nastran 2013. FEM includes secondary mirror (SM), SM linker, SM substrate, SM light shield, SM support, Primary mirror (PM), PM substrate, base plate and camera support structure which contains 56614 nodes, 35532 elements, 12 RBE2 and 1 CONM2. FEM is shown in Fig. 3.

Table 3. FE analysis results

Order	Frequency (Hz)	Modal formation			
	141.8	Support structure swing along X axis			
	156.4	Support structure swing along Y axis			
	320.7	Support structure rotation around the Z axis			
Direction	Input RMS (g)	Output response RMS of sample point (g)			
X -axis		15.2			
Y-axis	10.16	19.8			
Z -axis		23.3			

5. Experiments

To verify the feasibility of the size optimization method and the accuracy of the finite element numerical analysis results, we used the model vibration test bench (# MPA3436/H1859A) to test

the camera at room temperature according to conditions in Table 1. Test scene is shown in Fig. 4.

Curves of input, analysis and test of the random vibration response of the camera main support structure in the X -axis, Y -axis and Z -axis are shown in Fig. 5. The comparison of random vibration response test results and the analytical data are listed in Table 4.

Fig. 4. Placement of random vibration test

Fig. 5. Curves of input, analysis and test

Tapit T. Compare aad of losts and analysis (21ms)							
Axis	Input	Analysis result		Test result Relative errors	Relative magnification		
\mathcal{X}	0.16			3.8%	0.54		
	0.16	19.8	19.4	2.1%	0.91		
	0.16		22.4	40%			

Table 4. Compare data of tests and analysis (grms)

According to Table 4, the relative errors of random vibration response between finite element analysis results and vibration test data are less than 5 %, and the maximum relative magnification is 1.2 which is less than overall index 1.5. The results validate correctness of finite element models and feasibility of optimization methods in this paper.

6. Conclusions

Traditional optimization methods are mostly based on static mechanical properties parameters or frequency characteristics, which cannot directly optimize the dynamic parameters of the structure. In this paper, due to the RMS value of the acceleration response of the main support structure of the LQ-video satellite in Jilin-1 group satellites is too large under the random vibration excitation, the optimization design method based on the RMS value of the random response is proposed, and the following conclusions are got.

1) The mathematical model of random vibration response optimization is established, the modal and acceleration response sensitivity analysis of the model are carried out, and the optimal design of the main support structure is also provided. This method can provide a new idea for the design of other small satellite main structure.

2) The thickness of the main support structure of the camera is 2.5 mm and the distance between the support structure and mounting surface is 94.5 mm after size optimization, the random vibration acceleration response of the camera mounting position is minimum.

3) Engineering analysis and test results show that the main support structure of the camera is 141.8 Hz, which is larger than the overall index 110 Hz, and the maximal relative amplification rate of the support structure is 1.2, which is less than the overall design index 1.5. The main support structure of the camera performance parameters match the overall index well.

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