1804. Back-stepping variable structure controller design for off-road intelligent vehicle

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Abstract. In this paper, off-road path recognition and navigation control method are studied to realize intelligent vehicle autonomous driving in unstructured environment. Firstly, the traversable path is achieved by vision and laser sensors. The vehicle steering and driving coupled dynamic model is established. Secondly, a coordinated controller for steering and driving is proposed via the back-stepping variable structure control method, which can be used to deal with the unmatched uncertainties of the control system model. To reduce the chattering phenomenon caused by variable structure, the boundary layer approach is introduced. The results of simulation and off-road experiment show the effectiveness and robustness of the proposed controller.

Keywords: off-road intelligent vehicle, coordinated control, backstepping variable structure.

1. Introduction

Off-road intelligent vehicle has wide applications in the fields of military, civilian and planetary exploration. But the traversable off-road path is tortuous and undulates roughly without obvious marking. As a result, effectively path detection and tracking control become a challenging problem for off-road intelligent vehicle autonomous navigation.

For unstructured road detection field, the traversable path can be extracted by road features based method [1], road model based method [2] and learning based method [3] etc. Influenced by complex off-road environment and varying illumination conditions, fully reliable traversable path recognition cannot be achieved only depending on visual sensors.

Most research about tracking control of intelligent vehicle has focused on either pure longitudinal or pure lateral control [4-8]. For example, the longitudinal PI control method was extensively used for vehicle cruise control. Besides, the longitudinal controller can be designed based on the Lyapunov stability theory [9], or fuzzy-sliding mode control [10]. As for lateral controller design, basically using input-output feedback linearization [11], fuzzy theory [12-14], optimal control [15-16] and sliding-mode theory [17] based on preview model. In fact, there's tight coupling between the steering and driving dynamics of intelligent vehicle, and the coupling effects become increasingly significant especially in the off-road environment. As a result, to combine the longitudinal and lateral motion of off-road intelligent vehicle altogether, with parametric uncertainties, uncertain nonlinearities and external disturbances be concerned, a variable structure control approach based on backstepping is utilized in the paper. Besides, the chattering problem of variable structure is solved by introduce a saturation function.

2. Off-road path recognition

To realize navigation control of off-road intelligent vehicle, the desired path information need to be achieved real-time, from which the orientation deviation and lateral deviation from the preview point can be extracted. With the visual sensor and the assistant of laser sensor, the off-road path recognition is achieved and from which the desired path is extracted in the paper. The algorithm flow is shown in Fig. 1, the specific implementation steps are shown as follows:

1) Environmental information collection: the road image in front of the intelligent vehicle can be achieved through the color camera. In order to improve the reliability of the traveling regional discrimination, the convex obstacles in the road are detected based on the laser sensors. Through the pre-calibration, the correspondence relation between the laser data points and the image pixels is established.

2) Image preprocessing: The illumination compensation is made for the collected images to weaken the influence of illumination firstly. Then, the images are enhanced by histogram equalization to extract the road features. Finally, the convex obstacles region is marked to ensure that the seed points of the region-growing algorithm are selected automatically in the non-barrier region.



Fig. 1. Off-road path recognition flow chart

3) Texture feature extraction: As the texture can reflect the nature of image grey and the spatial relationship, the texture vector of the off-road image pixels is generated using the symbiosis matrix in this paper. The symbiosis matrix can reflect the summarized information of the image grey distribution on the direction, local neighborhood and the range of variation.

4) Region-growing based image segmentation: With the assistant of laser sensors, a traversable region near the front of the intelligent vehicle can be determined in the image. The region is taken as the road region, from which the seed points can be selected randomly. Region-growing can be conducted according to the similarity of texture and grey. Then the edges of road can be detected.

5) The extraction of desired trajectory: Morphological filter is applied for the segmented image firstly, after fill the cavity, filter the outlier, extract the Canny edge, then search the edge chain code from the image centre line to the image left and right side, get the length and the area information of the chain code, complete the left and right road edge identification. Finally, the road edge can be fitted and described by quadratic curves.

Fig. 2 shows some results of off-road path edge recognition. The right edge is taken as the desired trajectory that the intelligent vehicle needs to track in this paper, which provides the reliable and stable error feedback for the implementation of trajectory tracking control based on the vehicle preview kinematics and the driving dynamics.



Fig. 2. Some off-road path recognition results

3. Vehicle dynamics

Vehicle dynamics is a nonlinear dynamics system in presence of parametric uncertainties and strong coupling characteristics. The simplified model is derived under the following assumptions: 1) Neglect roll, pitch and vertical motion; 2) Discount the brake, throttle and steering dynamics; 3) Ignore the effect of suspension on the tire axles, and approximate the tire model as linearity. The resulting equations of the simplified vehicle model are:

$$\begin{split} \dot{v}_{x} &= -f_{R}g - \frac{c_{x}v_{x}^{2}}{m} + v_{y}\dot{\psi} + 2C_{f}\frac{v_{y} + l_{f}\dot{\psi}}{mv_{x}}\delta_{f} + \frac{1}{m}\frac{T_{e}i_{g}i_{o}\eta_{T}}{r_{w}} + g\sin\theta + \tau(\Delta_{x}), \\ \dot{v}_{y} &= -\frac{2(C_{f} + C_{r})}{mv_{x}}v_{y} - \left[v_{x} + \frac{2(C_{f}l_{f} - C_{r}l_{r})}{mv_{x}}\right]\dot{\psi} + \frac{2C_{f}}{m}\delta_{f} - \frac{c_{y}v_{y}^{2}}{m} + \tau(\Delta_{y}), \\ \ddot{\psi} &= -\frac{2(C_{f}l_{f}^{2} + C_{r}l_{r}^{2})}{I_{z}v_{x}}\dot{\psi} - \frac{2(C_{f}l_{f} - C_{r}l_{r})}{I_{z}v_{x}}v_{y} + \frac{2C_{f}l_{f}}{I_{z}}\delta_{f} + \tau(\Delta_{\psi}), \\ T_{e} &= MAP(w_{e}, a_{thr}), \end{split}$$
(1)

where v_x , v_y and ψ denote longitudinal velocity, lateral velocity, and yaw angle within a fixed inertial frame, respectively. *m* is total mass of the vehicle. I_z is total vehicle inertia about vertical axis at center of gravity (CG). l_f and l_r are the distance of the front and rear axles from the CG, respectively. c_x and c_y are longitudinal and lateral air resistance coefficients, respectively. f_R is rolling resistance coefficient. C_f and C_r are cornering stiffness of the front and rear tires, respectively. θ denotes the road grade, *g* denotes gravitational acceleration (m/s²). MAP is the steady-state engine map, δ_f denotes front wheel steering angle. T_e denotes engine torque, i_o is the final driver ratio, η_T denotes transmission coefficient, r_w denotes vehicle radius, i_g denotes automatic transmission gear ratio, w_e denotes engine speed, a_{thr} denotes throttle (%); $\tau(\Delta_x)$, $\tau(\Delta_y)$ and $\tau(\Delta_{\psi})$ denote uncertainties caused by unmodeled dynamics and time-varying parameters.

The model can be rewritten in canonical form:

$$\begin{split} \dot{v}_x &= f_0 + g_0 \delta_f + g_1 MAP(w_e, a_{thr}) + \tau(\Delta_x), \\ \dot{v}_y &= f_1 + g_2 \delta_f + \tau(\Delta_y), \\ \ddot{\psi} &= f_2 + g_3 \delta_f + \tau(\Delta_\psi), \end{split}$$
(2)

where:

$$\begin{aligned} f_0 &= -f_R g - \frac{c_x v_x^2}{m} + v_y \dot{\psi} + g \sin\theta, \ f_1 &= \frac{-2(C_f + C_r) v_y}{m v_x} - \left[v_x + \frac{2(C_f l_f - C_r l_r)}{m v_x} \right] \dot{\psi} - \frac{c_y v_y^2}{m}, \\ f_2 &= \frac{-2(C_f l_f^2 + C_r l_r^2) \dot{\psi}}{I_z v_x} - \frac{2(C_f l_f - C_r l_r) v_y}{I_z v_x}, \\ g_0 &= \frac{2C_f (v_y + l_f \dot{\psi})}{m v_x}, \ g_1 &= \frac{i_g i_o \eta_T}{m r_w}, \ g_2 &= \frac{2C_f}{m}, \ g_3 &= \frac{2C_f l_f}{I_z}. \end{aligned}$$

Assumption 1. The uncertain terms in dynamic model Eq. (1) are bounded, and there exists known continuous functions $a_i(v_x, v_y, \dot{\psi})$, (i = 1, 2, 3) which satisfy following conditions:

$$\tau(\Delta_x) \le a_1(v_x, v_y, \psi), \ \tau(\Delta_y) \le a_2(v_x, v_y, \psi), \ \tau(\Delta_{\psi}) \le a_3(v_x, v_y, \psi).$$
(3)

The basic principle of longitudinal control is to make the vehicle achieve expected speed/acceleration smoothly by adjusting the driving/braking torque according to control strategic.

Given a desired velocity v_p , actual velocity v_x , tracking velocity error v_e is defined as $v_e = v_x - v_p$ and the time derivative of v_e is obtained as:

$$\dot{v}_e = a_x - a_p,\tag{4}$$

where \dot{v}_e is the speed error rate, a_x and a_p are the actual acceleration and expected acceleration, respectively. The principle of lateral control is to make intelligent vehicles accurately track the reference road. Orientation error is defined as the angle between the vehicle centerline and reference road tangent at a specified look-ahead distance L, given by:

$$\dot{\phi}_e = v_x K_L - \dot{\psi},\tag{5}$$

where ϕ_e is the orientation error at look-ahead distance L, K_L is the road curvature.

Lateral error is the horizontal distance between the vehicle position and reference road at look-ahead distance, it can be described as:

$$\dot{y}_e = v_x \phi_e - v_y - \dot{\psi}L,\tag{6}$$

where y_e is the lateral error at a look-ahead distance.

Intelligent vehicles control system can be yielded by combining Eq. (2), Eq. (4), Eq. (5) and Eq. (6), and control system consisting of six state variables as v_e , y_e , ϕ_e , v_x , v_y , $\dot{\psi}$ and two control input variables as a_{thr} , δ_f , which has strict parameters state-feedback form.

4. Controller design

The lateral and longitudinal motion will be controlled when intelligent vehicles are driving, the target of lateral control is to make intelligent vehicle track the reference road, and the target of longitudinal control is to make speed error asymptotically converge to zero. As a result, variable structure control based on backstepping is utilized to guarantee globally uniformly ultimately bounded or global asymptotic stability of tracking errors.

Coordinated longitudinal and lateral control algorithm is designed as follows.

Step 1: Considering the lateral motion, the first error vector is defined as $s_{10} = y_e$. Choosing Lyapunov function as $V_{lat0} = 1/2s_{10}^2$, and the time derivative of V_{lat0} is obtained as:

$$\dot{V}_{lat0} = s_{10}\dot{s}_{10} = s_{10}\dot{y}_e = s_{10}(v_x\phi_e - v_y - \dot{\psi}L).$$
⁽⁷⁾

By setting $v_x \phi_e - \dot{\psi}L$ as virtual control input, the condition for y_e tends to zero is that \dot{V}_{lat0} must be negative definite such that $\dot{V}_{lat0} = -k_{11}s_{10}^2 \leq 0$, where k_{11} is a positive constant. Then the desired virtual control α_1 can be obtained as $\alpha_1 = -k_{11}s_{10} + v_y$. Defining the difference between the virtual control input $v_x \phi_e - \dot{\psi}L$ and its desired value α_1 to be the second error variable s_{11} , given by:

$$v_x \phi_e - \dot{\psi} L = s_{11} + \alpha_1.$$
 (8)

Substituting Eq. (8) to Eq. (7) yields:

$$\dot{V}_{lat0} = s_{10}s_{11} - k_{11}s_{10}^2. \tag{9}$$

Obviously when $s_{11} = 0$, $\dot{V}_{lat0} = -k_{11}s_{10}^2 \le 0$ is satisfied. The target of next step is to search the control input variables a_{thr} and δ_f which can make s_{11} converge to zero or a small value. Thus, s_{10} is guaranteed to converge to zero or be uniformly ultimately bounded.

Step 2: Choosing Lyapunov function as $V_{lat1} = V_{lat0} + 1/2 s_{11}^2$ and its time derivative can be obtained as:

$$\dot{V}_{lat1} = \dot{V}_{lat0} + s_{11}\dot{s}_{11} = -k_{11}s_{10}^2 + s_{10}s_{11} + s_{11}\dot{s}_{11}.$$
(10)

Let:

$$s_{10} + \dot{s}_{11} = -k_{12}s_{11}. \tag{11}$$

Substituting the time derivative of Eq. (8) to Eq. (11) yields:

$$s_{10} + \dot{v}_x \varphi_e + \dot{\varphi}_e v_x - \ddot{\psi} L - \dot{\alpha}_1 = -k_{12} s_{11}.$$
(12)

Substituting $\dot{\alpha}_1 = -k_1 \dot{s}_1 + \dot{v}_y$, $\dot{\psi}_x$, $\ddot{\psi}$, \dot{v}_y to Eq. (12) yields:

$$-k_{12}s_{11} = s_{10} + (f_0 + g_0\delta_f + g_1MAP(w_e, a_{thr}))\phi_e + \dot{\phi}_e v_x - (f_2 + g_3\delta_f)L + k_{11}\dot{s}_{10} - (f_1 + g_2\delta_f) + \eta_1.$$
(13)

We can get $\dot{V}_{lat1} = -k_{11}s_{10}^2 - k_{12}s_{11}^2 \le 0$, where k_{12} is positive constant, η_1 is the uncertain term that caused by the time derivative of s_{11} . According to the assumption 1, there exists known continuous positive function $\beta_1(v_x, v_y, \dot{\psi})$, which satisfies $\eta_1 \le \beta_1(v_x, v_y, \dot{\psi})$.

Step 3: Considering the longitudinal motion, the error vector is defined as $s_{20} = v_e$. Choosing Lyapunov function as $V_{logit0} = 1/2 s_{20}^2$, and $\dot{V}_{logit0} = s_{20}\dot{s}_{20} = s_{20}\dot{v}_e = s_{20}(a_x - a_p)$. The condition for s_{20} tends towards zero is that \dot{V}_{logit0} must be negative definite such that $\dot{V}_{logit0} = -k_{21}s_{20}^2 \le 0$.

Let $f_0 + g_0 \delta_f + g_1 MAP(MAP(w_e, a_{thr})) + \eta_2 - \dot{v}_p = -k_{21}s_{20}$, where k_{21} is a positive constant, η_2 is the uncertain term which caused by the time derivative of s_{21} . s_{21} is the time derivative of s_{20} . According to the assumption 1, there exists known continuous positive function $\beta_2(v_x, v_y, \dot{\psi})$, which satisfies $\eta_2 \leq \beta_2(v_x, v_y, \dot{\psi})$.

Then, an equivalent control is obtained as:

$$\mathbf{u}_{eq} = \begin{bmatrix} T_{eeq} \\ \delta_{feq} \end{bmatrix} = \begin{bmatrix} g_1 & g_0 \\ g_1 \phi_e & (g_0 \phi_e - g_2 - g_3 L) \end{bmatrix}^{-1} \begin{bmatrix} \sigma_1 \\ \sigma_2 \end{bmatrix},\tag{14}$$

where T_{eeq} is equivalent engine torque, δ_{feq} is equivalent front wheel steering angle. With:

$$\sigma_{1} = -f_{0} + \dot{v}_{p} - k_{21}s_{20} - \frac{s_{20}\beta_{2}^{2}}{2\varepsilon_{2}},$$

$$\sigma_{2} = -s_{10} - f_{0}\varphi_{e} - \dot{\varphi}_{e}v_{x} + f_{2}L + f_{1} - k_{11}\dot{s}_{10} - k_{12}s_{11} - \frac{s_{11}\beta_{1}^{2}}{2\varepsilon_{1}},$$

where $-s_{20}\beta_2^2/2\varepsilon_2$, $-s_{11}\beta_1^2/2\varepsilon_1$ are nonlinear damping terms, which are designed to compensate for the disturbance of uncertain terms η_1 , η_2 . ε_1 and ε_2 are positive constant, respectively.

Choosing variable structure control law using bounded layer approach as:

$$u_{s} = \begin{cases} \lambda_{2}sat\left(\frac{s_{11}}{\Delta_{2}}\right), \\ \lambda_{1}sat\left(\frac{s_{20}}{\Delta_{1}}\right), \end{cases}$$
(15)

where:

$$\begin{cases} sat\left(\frac{s_{11}}{\Delta_2}\right),\\ sat\left(\frac{s_{20}}{\Delta_1}\right), \end{cases}$$

is saturation function. $\Delta_1 > 0$ and $\Delta_2 > 0$ denote thickness of boundary layer. λ_1 and λ_2 are positive constant, respectively.

Consequently, coordinated longitudinal and lateral control law can be expressed as:

$$\mathbf{u} = \begin{bmatrix} T_{ed} \\ \delta_{fd} \end{bmatrix} = u_{eq} + u_s = \begin{bmatrix} T_{eeq} + T_{es} \\ \delta_{feq} + \delta_{fs} \end{bmatrix}.$$
(16)

 T_{ed} and δ_{fd} are the desire engine torque and front wheel steering angle, respectively. According to $T_e = MAP(\omega_e, \alpha_{thr})$ we can get:

$$\alpha_{thrd} = MAP^{-1}(\omega_e, T_{ed}). \tag{17}$$

The α_{thrd} denotes desired throttle (%). From Eq. (16), δ_{fd} is obtained as:

$$\delta_{fd} = \delta_{feq} + \delta_{fs} = \delta_{feq} + \lambda_2 sat\left(\frac{s_{11}}{\Delta_2}\right).$$
(18)

 δ_{feq} and T_{eeq} satisfy the following equation:

$$(f_0 + g_0 \delta_{\text{feq}} + g_1 T_{eeq}) \varphi_e + \dot{\varphi}_e v_x - (f_2 + g_3 \delta_{\text{feq}}) L + k_{11} \dot{s}_{10} - (f_1 + g_2 \delta_{feq})$$

= $-s_{10} - k_{12} s_{11} - \frac{s_{11} \beta_1^2}{2\varepsilon_1}.$ (19)

Then, the graphical diagram of the controller design is given in Fig. 3.



Fig. 3. Graphical diagram of the controller

5. Stability analysis

To investigate the stability of the proposed controller, the time derivative of Eq. (8) is substituted to Eq. (10) yields:

$$\begin{aligned} \dot{V}_{lat1} &= -k_{11}s_{10}^2 + s_{10}s_{11} + s_{11}\dot{s}_{11} \\ &= -k_{11}s_{10}^2 + s_{10}s_{11} + s_{11}(\dot{v}_x\phi_e + \dot{\phi}_e v_x - \ddot{\psi}L - \dot{\alpha}_1) \\ &= -k_{11}s_{10}^2 + s_{10}s_{11} + s_{11}((f_0 + g_0\delta_f + g_1T_e)\phi_e + \dot{\phi}_e v_x \\ &- (f_2 + g_3\delta_f)L + k_{11}\dot{s}_{10} - (f_1 + g_2\delta_f) + \eta_1). \end{aligned}$$
(20)

Let $\delta_f = \delta_{fd}$, $T_e = T_{eeq}$. Substituting Eq. (19) to Eq. (20) yields:

$$\begin{split} \dot{V}_{lat1} &= -k_{11}s_{10}^{2} + s_{10}s_{11} + s_{11}\left(-s_{10} - k_{12}s_{11} - \frac{s_{11}\beta_{1}^{2}}{2\varepsilon_{1}} + \eta_{1}\right) \\ &+ s_{11}\lambda_{2}(g_{0}\phi_{e} - g_{2} - g_{3}L)sat\left(\frac{s_{11}}{\Delta_{2}}\right) = -k_{11}s_{10}^{2} - k_{12}s_{11}^{2} - \frac{s_{11}^{2}\beta_{1}^{2}}{2\varepsilon_{1}} + \eta_{1}s_{11} \\ &+ s_{11}\lambda_{2}(g_{0}\phi_{e} - g_{2} - g_{3}L)sat\left(\frac{s_{11}}{\Delta_{2}}\right). \end{split}$$

$$(21)$$

Due to $\eta_1 \leq \beta_1$, we use the method of balance for $-s_{11}^2 \beta_1^2 / 2\varepsilon_1 + \eta_1 s_{11}$, then can get:

$$-\frac{s_{11}^2\beta_1^2}{2\varepsilon_1} + \eta_1 s_{11} \le -\left(\frac{s_{11}\beta_1}{\sqrt{2\varepsilon_1}} - \frac{\sqrt{\varepsilon_1}}{\sqrt{2}}\right)^2 + \frac{\varepsilon_1}{2} \le \frac{\varepsilon_1}{2}.$$
(22)

Let $k_{12} > k_{11}$, $\kappa = \lambda_2 (g_0 \phi_e - g_2 - g_3 L) / \Delta_2$, the final equation is obtained as:

$$\begin{split} \dot{V}_{lat1} &\leq -k_{11}s_{10}^2 - k_{11}s_{11}^2 - (k_{12} - k_{11})s_{11}^2 + \frac{\varepsilon_1}{2} + \kappa |s_{11}| \\ &= -2k_{11}V_{lat1} - (k_{12} - k_{11})s_{11}^2 + \frac{\varepsilon_1}{2} + \kappa |s_{11}| \\ &\leq -2k_{11}V_{lat1} - \left(\sqrt{k_{12} - k_{11}}|s_{11}| - \frac{\kappa}{2\sqrt{k_{12} - k_{11}}}\right)^2 \frac{\varepsilon_1}{2} - \frac{\kappa^2}{4(k_{12} - k_{11})} \\ &\leq -2k_{11}V_{lat1} + \frac{\varepsilon_1}{2}. \end{split}$$

$$(23)$$

We can get $\lim_{t\to\infty} V_{lat1} \le \varepsilon_1/4k_{11}$, it can be proved that error vector s_{10} is uniformly ultimately bounded. Similarly, the error vector s_{20} is uniformly ultimately bounded.

6. Simulation and experiment

To examine the performance of proposed control algorithms, numerical simulation tests and experiment were performed. Fig. 4 shows the experimental prototype and test environment, and the test road has changing slope and curvature, with the main features of off-road environment. Table 1 shows the main parameters of the vehicle.



Fig. 4. Experimental platform

Parameters	Nominal value
m	2100 kg
I_z	3059 kg·m ²
l_f	1.1 m
l_r	1.4 m
i _o	3.86
C_f, C_r	37500 Kn/rad
η_T	0.99
r_w	0.33 m
f_r	0.02
i_g	0.79

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The road curvature, desired velocity and acceleration profile used in simulation test are shown in Fig. 5, respectively. The initial lateral error is 0.1m, the initial orientation error is 0.02 rad, and the initial velocity error is 0.5 m/s. Fig. 6 shows the simulation results of backstepping variable structure, Fig. 6(a) is the response curve of lateral error, Fig. 6(b) is the response curve of velocity error, Fig. 6(a) and Fig. 6(b) show that lateral error and longitudinal error all can asymptotically converges to zero when the road curvature and traction acceleration change, and the controller has a strong capability of anti-disturbance and excellent robustness. Fig. 6(c) is the response curve of orientation error, and orientation error can asymptotically converge to zero when road curvature is zero. The steady-state error of orientation error larger when road curvature becomes larger, but orientation errors converged to acceptable bounds.



0.03

Road curvature(m¹ 10⁰

-0.01 --0.02 -

 Table 1. Main vehicle parameters

c) Expected acceleration Fig. 5. Road curvature and desired velocity

30 t/s

-0.1

To demonstrate the advantages of the proposed controller, the traditional longitudinal PI controller and lateral optimal controller have been designed for comparison under the same road curvature, desired velocity and acceleration profile in Fig. 5. Firstly, the control parameter of PI controller was adjusted to make the velocity error reach the same adjustment time and control accuracy in Fig. 6(b); then, the weighting coefficient of the optimal controller to make the lateral error reach the same control level in Fig. 6(a), and the corresponding orientation error is shown in

Fig. 7. It can be seen that there are significant rises in orientation error and overshoot which may lead the frequent chattering problem of steering wheel and reduce the riding comfort in the vehicle's navigation. By contrast, as the algorithm proposed in this paper introduced a saturation function in the variable structure control, the lateral control of the vehicle is softer and the chattering problem is solved.



c) The response curve of orientation error **Fig. 6.** Simulation results of backstepping variable structure controller



Fig. 7. The response curve of orientation error under the traditional longitudinal PI controller and lateral optimal controller

Fig. 8 shows the experimental results of the proposed controller in this paper, expected velocity is 15 km/h, The test road is rugged and includes not only the change with slope and curvature of the path, but also a certain sensor measurement error and noise, Fig. 6 demonstrate that proposed controller have good performance in the off-road environment.

7. Conclusion

The paper has presented the coupled steering and driving dynamics for off-road intelligent vehicle, and a back-stepping variable structure controller has been designed. Both simulation and experimental tests have been carried out and the results have been given. These results indicate that the proposed control strategy achieve good command tracking performance in the off-road environment.



Fig. 8. Experimental results of back-stepping variable structure controller

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